| x | $\log _{2}(P(\mathbf{x}))$ |
| :---: | :---: |
| ..1...............1....1...1.1......1......1.........1..................1......11... | . -50.1 |
| ...1....1....1......1...1.......1................................1... | . -37.3 |
| .1...1.1...1...11..1.1.......11.....................1..1.1..1...1.............. 1. | . -65.9 |
| 1.1..1.............1....................11.1.1........................1....1.1.11.... | . -56.4 |
| ...11.........1..1....1.1.....1........1...1..1....1..........1.................... | . -53.2 |
| .1.....1.......1.1......1........1..........1..1...................1...... | - -43.7 |
| ....1......1.....1..1.........1.........1.........1.....1.11.................... | . -46.8 |
| ....1..1.1............111...............1............1.......1.1...1...1........... 1 | $1-56.4$ |
| ..1........1....1.....1........1...1.....................................1... | . -37.3 |
| .....1......................1..............1....1..1.1.1.1.....................................1. | . -43.7 |
| 1.....................1.........1..1..................1...1...1........1.11..1.1..1........ | $-56.4$ |
| 11.1.........1. $\qquad$ .1...... 1. <br> . 1. | . -37.3 |
| .1........1..1.1..........1.....11........1.1...1...........1..........11........ | . -56.4 |
| .....1..1..1....1.11.1.1.1..1..................1..........1...........1.1............ | . -59.5 |
| ....11.1.....1...1..1........................1......1............1......1........ | . -46.8 |
|  | . -15.2 |
| 1111111111111111111111111111111111111111111111111111111111111111111111111111111111111111111111111111 | $1-332.1$ |

Figure 4.10. The top 15 strings are samples from $X^{100}$, where $p_{1}=0.1$ and $p_{0}=0.9$. The bottom two are the most and least probable strings in this ensemble. The final column shows the log-probabilities of the random strings, which may be compared with the entropy $H\left(X^{100}\right)=46.9$ bits.
$n(r)=\binom{N}{r}$

$P(\mathbf{x})=p_{1}^{r}\left(1-p_{1}\right)^{N-r}$
$\log _{2} P(\mathbf{x})$


$n(r) P(\mathbf{x})=\binom{N}{r} p_{1}^{r}\left(1-p_{1}\right)^{N-r}$

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0.045
0.04
0.035
0.03
0.025
0.02
0.015
0.01
0.005
0.04
0.035
0.03
0.025
0.02
0.02
0.015
0.01
0.005
0 $0-1.1$
 dom variables each with entropy $H(X)$ can be compressed into more than $N H(X)$ bits with negligible risk of information loss, as $N \rightarrow \infty$; conversely if they are compressed into fewer than $N H(X)$ bits it is virtually certain that information will be lost.

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at least $H-\epsilon$ bits. These two extremes tell us that regardless of our specific allowance for error, the number of bits per symbol needed to specify $\mathbf{x}$ is $H$ bits; no more and no less.

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