

general relativity – February 17, 2011

material discussed in class

Roughly 3.4, 3.6, 3.7, 3.8 in the book (didn't do all of it though).

exercises

- Show that

$$[\nabla_\mu, \nabla_\nu]V_\rho = -R^\sigma{}_{\rho\mu\nu}V_\sigma \quad (1)$$

given that

$$[\nabla_\mu, \nabla_\nu]V^\rho = R^\rho{}_{\sigma\mu\nu}V^\sigma. \quad (2)$$

- What would be the answer for $[\nabla_\mu, \nabla_\nu]A^\alpha{}_{\beta\gamma}$? Don't compute this explicitly, but use properties of the covariant derivative to figure out what the answer should be.
- Find a set of coordinates on the two-sphere which define a local inertial frame near the point $(\theta, \phi) = (\pi/2, 0)$ on the equator.
- Prove that any geodesic on the two-sphere always follows a 'big circle', i.e. a circle obtained by intersecting the two-sphere by a two-plane which passes through the origin. Here we view the two-sphere as the sphere $x^2 + y^2 + z^2 = R^2$ in \mathbb{R}^3 .