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Higgs

From prediction to discovery and beyond



Content

- Theory
- Search for Higgs at LHC
- Experimental verification of Higgs
- Higgs beyond the standard model





Theory

- Electroweak model
- Problems
- Higgs mechanism
- Higgs decay channels





The gauge principle

- QFT framework: inherent redundancy
- Demand: local gauge invariance
- Led to QED





QED

Dirac Lagrangian

$$L_{Dirac} = \overline{\psi}(i\not\partial - m)\psi$$

Euler Lagrange

Dirac Equation

$$\left(i\not\partial -m\right)\psi=0$$

QED

 Demand invariance of Lagrangian under the local U(1) rotation

 $\psi(x) \to e^{iea(x)}\psi(x)$

• Introduce covariant derivative $\partial_{\mu} \rightarrow D_{\mu} = \partial_{\mu} + eA^{\mu}(x)$

 \blacksquare With the field A_{μ} , which transforms as:

$$A^{\mu} \to A^{\mu} = A^{\mu} - \frac{1}{e} \partial_{\mu} \alpha(x)$$



$$L_{Dirac} = \overline{\psi}(i\not\partial - m)\psi$$



QED

$$L_{Dirac} = \overline{\psi}(i\not\partial - m)\psi$$

Minimal substitution leads to local gauge invariant (interacting) theory:

$$\begin{split} L_{Dirac} &= L_{freeDirac} + L_{interaction} \\ L_{Dirac} &= \overline{\psi} \left(i \not D - m \right) \psi \\ &= \overline{\psi} \left(i \not \partial - m \right) \psi + e \overline{\psi} \gamma_{\mu} A^{\mu}(x) \psi \end{split}$$



Introducing the electroweak model

Main Ingredients:

- Local (non-abelian) gauge invariance
- Renormalizability (puts restrictions on the possible terms in Lagrangian)
- Spontaneous symmetry breaking









Massless electroweak model SU(2), XU(1),

- Weak interaction on LH doublets (maximal violation of parity).
- Fermionic content:

$$\psi_L = \begin{pmatrix} \psi^0 \\ \psi^- \end{pmatrix}_L \qquad \psi_R$$

Action of SU(2) and U(1):

$$\psi_L \xrightarrow{SU(2)_L \times U(1)_Y} e^{i\vec{\beta}\cdot\vec{T}} e^{i\alpha Y} \psi_L$$

$$\psi_R \xrightarrow{SU(2)_L \times U(1)_Y} 1 \cdot e^{i\alpha Y} \psi_R$$



From global to local SU(2)xU(1)

For each symmetry generator of the gauge group, a gauge fields to construct a covariant derivative is introduced:

• For doublets (L):
$$\partial_{\mu} \rightarrow D_{\mu} = \partial_{\mu} - W_{\mu} + B_{\mu}$$

For singlets (R):

$$\partial_{\mu} \longrightarrow \nabla_{\mu} = \partial_{\mu} + B_{\mu}$$



Electroweak Lagrangian

Minimal substitution in free electroweak theory:

 $L_{EW} = \overline{\psi}_L \not\!\!\!\! D_\mu \psi_L + \overline{\psi}_R \not\!\!\! \nabla_\mu \psi_R$

Kinetic gauge terms:

$$L_{kinetic} = -\frac{1}{4} W_a^{\mu\nu} W_{\mu\nu}^a - \frac{1}{4} B^{\mu\nu} B_{\mu\nu}$$

| Fermions matter particles | Gauge bosons force carriers |
|------------------------------|--------------------------------|
| Quarks | photon |
| d 😮 🕩 | Z0 Z boson |
| Leptons $v_e v_\mu v_\tau$ | W boson |
| e 🔉 र | |



Two main problems

- Mass terms lead to explicit breaking of symmetry:
- Fermion mass -> global (thus local) gauge variance
- Gauge boson mass -> Non-renormalizability +global gauge variance



Problems with SM

• Fermion mass term: $m\overline{\psi}\psi = m(\overline{\psi}_R\psi_L + \overline{\psi}_L\psi_R)$ $\overline{\psi}_R\psi_L + \overline{\psi}_L\psi_R \rightarrow$ $(\overline{\psi}_R e^{-i\beta Y})(e^{i\vec{\alpha}\cdot\vec{T}}e^{i\beta Y}\psi_L) + (\overline{\psi}_L e^{-i\beta Y}e^{-i\vec{\alpha}\cdot\vec{T}})(e^{i\beta Y}\psi_R)$

• Gauge boson mass term: $m \vec{W}_{\mu} \cdot \vec{W}^{\mu} + m B^{\mu} B_{\mu}$ $W^{a}_{\mu} \rightarrow W^{a}_{\mu} + g \varepsilon_{abc} W^{b}_{\mu} \alpha^{c} + \partial_{\mu} \alpha^{a}$ $B_{\mu} \rightarrow B_{\mu} + \partial_{\mu} \beta$



Non-renormalizability

- Interatctions of longitudinal polarizations of W bosons lead to divergences
- Divergence soothened by exchange of Higgs boson



Solution of problems

Spontaneous symmetry breaking

- Spontaneous = ground state is not invariant under (gauge) symmetry of theory
- Hidden gauge symmetry in stead of broken gauge symmetry $\phi(x) = v + h(x)$





Goldstones

- Global spontaneously broken symmetries lead to the appearance of massless goldstone bosons
- Local broken symmetries give massless gauge bosons mass. The massless gauge bosons 'eat' the massless goldstones to provide for the missing degree of freedom.



Global breakdown

• Start with theory of a complex scalar $L = \partial_{\mu} \phi \partial_{\mu} \phi^* - V(|\phi|)$

 Assume the complex scalar has non zero vev (potential has a global minimum at the non-zero expectation value)

$$\langle |\phi| \rangle = a$$
 with $V(a) = 0$

Famous mexican hat potential





Global breakdown

Naturally expanding

$$\phi(x) = a + \eta_1(x) + i\eta_2(x)$$

- lacksquare This leads to a lagrangian with a massive $oldsymbol{\eta}_1$ and massless $oldsymbol{\eta}_2$
- Goldstone not observed in nature!



Abelian Higgs model

 Consider a charged scalar minimally coupled to an abelian gauge field:

$$L = D_{\mu} \phi D_{\mu} \phi^* - V(|\phi|)$$

 Assume the complex scalar has non zero vev (potential has a global minimum at the non-zero expectation value)

 Local U(1) invariance can be used to make real (unitary gauge) :

$$\phi^*(x) = \phi(x)$$

Massless goldstone is 'eaten' by gauge field



Abelian Higgs model

- Spontaneous breaking: $<\phi>=v$ with V(v)=0
- To analyze the particle spectrum of the theory, it is natural to redefine our field:

 $\phi(x) = v + h(x)$

Expanding Lagrangian leads to:

$$L_{U(1)+higgs} = D_{\mu}\phi D_{\mu}\phi^{*} - V(\phi)$$

= ... + $(\partial_{\mu} + B_{\mu})(v+h)(\partial_{\mu} + B_{\mu})(v+h) - V(v+h)$



Conclusion

- Massless goldstone is eaten and the massless goldstone has been eaten by the Higgs
- Coupling scalar to gauge fields with non-zero vev, we can create massive gauge bosons, while respecting gauge symmetries of theory.

Massive electroweak sector

 Analogous to Abelian Higgs model now the Higgs SU(2) doublet couples to an abelian field

$$\Phi = \begin{pmatrix} \phi_1 + i\phi_2 \\ \phi_3 + i\phi_4 \end{pmatrix} = \begin{pmatrix} 0 \\ v+h \end{pmatrix} \quad L = D_\mu \Phi D_\mu \Phi^* - V(|\Phi|)$$

 Use SU(2) gauge freedom to gauge in one direction of 4space.

3 goldstones dissappear from doublet, but reappear as parameters of rotated (gauged) gauge fields.

Higgs doublet transforms sunder SU(2)xU(1) in order to make fermion mass terms invariant as we will see later



1

Degrees of freedom

Degrees of freedom are redistributed:

| 4 massless gauge bosons | S = 1 | 4x2 |
|-------------------------|-------|-----|
| 4 Higgs scalars | s = 0 | 4x1 |
| 3 massive gauge bosons | s = 1 | 3x3 |
| 1 massless gauge boson | s = 1 | 1x2 |
| | | |

1 massive higgs scalar s = 0

Masses of the Gauge bosons

Local gauge invariant Lagrangian with mass:

$$L_{Higgs} = D_{\mu} \Phi^{\dagger} D_{\mu} \Phi + h.c.$$

= $(\partial_{\mu} - W_{\mu} + B_{\mu}) (0 \quad v + h) (\partial_{\mu} - W_{\mu} + B_{\mu}) \begin{pmatrix} 0 \\ v + h \end{pmatrix}$
= $\frac{1}{8} v^{2} (W_{\mu}^{+2} + W_{\mu}^{-2} + Z_{\mu}^{-2} + 0 \cdot A_{\mu}) + hVV + h^{3} + h^{4}$

• Assuming $v = 246 \, GeV$

$$Mw + = Mw - = \frac{1}{2}vg = 80.4 \,GeV$$
$$Mz = \frac{1}{2}v\sqrt{g^2 + g'^2} = 91.2 \,GeV$$



Yukawa Lagrangian

Bonus of Higgs theory:

- Massive fermions AND fermion higgs interaction
- However the mass value is not predicted in SM.

$$L_{Yukawa} = \overline{\psi}_L \Phi \psi_R + h.c.$$
$$= \overline{\psi}_L \begin{pmatrix} 0\\ v+h \end{pmatrix} \psi_R + h.c.$$

Yukawa Lagrangian



$$\begin{aligned} \mathcal{L}_{e} &= -\lambda_{e} \frac{1}{\sqrt{2}} \left[(\bar{\nu}, \bar{e})_{L} \begin{pmatrix} 0 \\ v+h \end{pmatrix} e_{R} + \bar{e}_{R}(0, v+h) \begin{pmatrix} \nu \\ e \end{pmatrix}_{L} \\ &= -\frac{\lambda_{e}(v+h)}{\sqrt{2}} [\bar{e}_{L}e_{R} + \bar{e}_{R}e_{L}] \\ &= -\frac{\lambda_{e}(v+h)}{\sqrt{2}} \bar{e}e \\ &= -\frac{\lambda_{e}v}{\sqrt{2}} \bar{e}e & -\frac{\lambda_{e}}{\sqrt{2}} h \bar{e}e \\ &\text{electron mass term electron-higgs interaction} \\ &m_{e} = \frac{\lambda_{e}v}{\sqrt{2}} & \frac{\lambda_{e}}{\sqrt{2}} \propto m_{e} \end{aligned}$$

The Standard model is a QFT with a Lagrangian invariant under local symmetries:

Gauge group $SU(3)_C \otimes SU(2)_L \otimes U(1)_Y$

Fermionic sector 5 representations of the zoo of particles (s=1/2) Scalar sector Higgs particle (s=0) LGI requires 3 gauge boson fields G, W, B (s=1)

Extra observed global symmetries B Baryon number L Lepton number

SM Lagrangian

$$\mathcal{L} = -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{8} tr(\mathbf{W}_{\mu\nu} \mathbf{W}^{\mu\nu}) - \frac{1}{2} tr(\mathbf{G}_{\mu\nu} \mathbf{G}^{\mu\nu})$$
 (U(1), SU(2) and SU(3) gauge terms)

$$+ (\bar{\nu}_L, \bar{e}_L) \bar{\sigma}^{\mu} i D_{\mu} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} + \bar{e}_R \sigma^{\mu} i D_{\mu} e_R + \bar{\nu}_R \sigma^{\mu} i D_{\mu} \nu_R + (h.c.)$$
 (lepton dynamical term)

$$- \frac{\sqrt{2}}{v} \left[(\bar{\nu}_L, \bar{e}_L) \phi M^e e_R + \bar{e}_R \bar{M}^e \bar{\phi} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} \right]$$
 (electron, muon, tauon mass term)

$$- \frac{\sqrt{2}}{v} \left[(-\bar{e}_L, \bar{\nu}_L) \phi^* M^{\nu} \nu_R + \bar{\nu}_R \bar{M}^{\nu} \phi^T \begin{pmatrix} -e_L \\ \nu_L \end{pmatrix} \right]$$
 (neutrino mass term)

$$+ (\bar{u}_L, \bar{d}_L) \bar{\sigma}^{\mu} i D_{\mu} \begin{pmatrix} u_L \\ d_L \end{pmatrix} + \bar{u}_R \sigma^{\mu} i D_{\mu} u_R + \bar{d}_R \sigma^{\mu} i D_{\mu} d_R + (h.c.)$$
 (quark dynamical term)

$$- \frac{\sqrt{2}}{v} \left[(\bar{u}_L, \bar{d}_L) \phi M^d d_R + \bar{d}_R \bar{M}^d \bar{\phi} \begin{pmatrix} u_L \\ d_L \end{pmatrix} \right]$$
 (down, strange, bottom mass term)

$$- \frac{\sqrt{2}}{v} \left[(-\bar{d}_L, \bar{u}_L) \phi^* M^u u_R + \bar{u}_R \bar{M}^u \phi^T \begin{pmatrix} -d_L \\ u_L \end{pmatrix} \right]$$
 (up, charmed, top mass term)

$$+ (\bar{D}_\mu \phi) D^\mu \phi - m_h^2 [\bar{\phi} \phi - v^2/2]^2 / 2v^2.$$
 (Higgs dynamical and mass term) (1)

where (h.c.) means Hermitian conjugate of preceeding terms, $\bar{\psi} = (h.c.)\psi = \psi^{\dagger} = \psi^{*T}$, and the derivative operators are

$$D_{\mu} \begin{pmatrix} \nu_L \\ e_L \end{pmatrix} = \left[\partial_{\mu} - \frac{ig_1}{2} B_{\mu} + \frac{ig_2}{2} \mathbf{W}_{\mu} \right] \begin{pmatrix} \nu_L \\ e_L \end{pmatrix}, \quad D_{\mu} \begin{pmatrix} u_L \\ d_L \end{pmatrix} = \left[\partial_{\mu} + \frac{ig_1}{6} B_{\mu} + \frac{ig_2}{2} \mathbf{W}_{\mu} + ig \mathbf{G}_{\mu} \right] \begin{pmatrix} u_L \\ d_L \end{pmatrix}, \tag{2}$$

$$D_{\mu}\nu_{R} = \partial_{\mu}\nu_{R}, \quad D_{\mu}e_{R} = \left[\partial_{\mu} - ig_{1}B_{\mu}\right]e_{R}, \quad D_{\mu}u_{R} = \left[\partial_{\mu} + \frac{i2g_{1}}{3}B_{\mu} + ig\mathbf{G}_{\mu}\right]u_{R}, \quad D_{\mu}d_{R} = \left[\partial_{\mu} - \frac{ig_{1}}{3}B_{\mu} + ig\mathbf{G}_{\mu}\right]d_{R}, \quad (3)$$

$$D_{\mu}\phi = \left[\partial_{\mu} + \frac{ig_1}{2}B_{\mu} + \frac{ig_2}{2}\mathbf{W}_{\mu}\right]\phi.$$
(4)

 ϕ is a 2-component complex Higgs field. Since \mathcal{L} is SU(2) gauge invariant, a gauge can be chosen so ϕ has the form

$$\phi^T = (0, v+h)/\sqrt{2}, \qquad \langle \phi \rangle_0^T = (\text{expectation value of } \phi) = (0, v)/\sqrt{2}, \qquad (5)$$

where v is a real constant such that $\mathcal{L}_{\phi} = \overline{(\partial_{\mu}\phi)}\partial^{\mu}\phi - m_{h}^{2}[\bar{\phi}\phi - v^{2}/2]^{2}/2v^{2}$ is minimized, and h is a residual Higgs field. B_{μ} , \mathbf{W}_{μ} and \mathbf{G}_{μ} are the gauge boson vector potentials, and \mathbf{W}_{μ} and \mathbf{G}_{μ} are composed of 2×2 and 3×3 traceless Hermitian matrices. Their associated field tensors are

$$B_{\mu\nu} = \partial_{\mu}B_{\nu} - \partial_{\nu}B_{\mu}, \quad \mathbf{W}_{\mu\nu} = \partial_{\mu}\mathbf{W}_{\nu} - \partial_{\nu}\mathbf{W}_{\mu} + ig_2(\mathbf{W}_{\mu}\mathbf{W}_{\nu} - \mathbf{W}_{\nu}\mathbf{W}_{\mu})/2, \quad \mathbf{G}_{\mu\nu} = \partial_{\mu}\mathbf{G}_{\nu} - \partial_{\nu}\mathbf{G}_{\mu} + ig(\mathbf{G}_{\mu}\mathbf{G}_{\nu} - \mathbf{G}_{\nu}\mathbf{G}_{\mu}).$$
(6)

Couplings to higgs $h \to f\overline{f}$





The end of a Higgs boson



 $(h \to q.loop \to g\overline{g}) = \alpha_s^2 N_c \frac{m_l^3}{m_h} [1 + \alpha_s + ...]^2$





Implication of branching ratios

- They strongly depends on higgsmass
- Strongly influences the detectability along certain channels
- WW for example can be not present or most dominant



Experimental constraints

- The Large Hadron Collider (LHC) have excluded the mass region below 114.4 GeV
- Tevatron and the LHC excluded a boson below 600 GeV, apart from mass regions 116 to 127 GeV.
- The CDF and DØ experiments at the Tevatron have also recently reported a broad excess in the mass region 120–135 GeV





Decay of 125 GeV Higgs

- For $M_h = 125$ GeV we can calculate branching ratios
- All 5 decay channels are significantly pressent





Properties of the channels

- $H \rightarrow ZZ^* \rightarrow 4I$ and $H \rightarrow \gamma \gamma give narrow mass peaks$
- $H \rightarrow ZZ^* \rightarrow 4I$, $H \rightarrow \gamma\gamma$ and $H \rightarrow WW^* \rightarrow e\nu\mu\nu$ more sensitive than bb and tt (less background)
- Diphoton final state implies that the boson has an integer spin different from unity.
- Decay to W bosons are harder to precisely reconstruct because of undected neutrino's

Large Hadron Collider (LHC)




Properties LHC

- The energy \sqrt{s} is distributed statistically over six quarks
- What particles can actually be measure?
- Each detection indentifies the energy, impuls and charge of the particle.
- In all directions particle can be measured except In longitudinal direction for angles smaller than .8 deg



Higgs production at LHC

- Largest SM higgs production cross sections:
 - Gluon fusion gg -> H (ggF)
 - W or Z boson fusion qq -> qqH (VBF)
 - Associated production production with W or Z bosons qq -> VH (VH)
- All production processes add up to a total cross section for Higgs.



How many collisions

- Integrated luminosity of 5.3 fb⁻¹ (7.6 10³³ cm⁻² s^{-1,} ∫Ldt)
- Integrated luminosity multiplied with total cross section gives expected number Higgs creations
- 10⁵ Higgs particles expected for 5.3 fb⁻¹ including all channels



Trigger

- From 10⁹ events/s to 200 event/s
- Multi levels of triggering
- Using 1 hardware trigger and 2 software triggers

 Hardware, 3µs, 10⁵ event/s
Software 40 ms 2000 event/s
Software 4s 200 event/s



Background at the LHC

- Reducible Vs Irreducible
- Processes contributing to background events

Table 1: Event generators used to model the signal and background processes. "PYTHIA" indicates that PYTHIA6 and PYTHIA8 are used for simulations of $\sqrt{s} = 7 \text{ TeV}$ and $\sqrt{s} = 8 \text{ TeV}$ data, respectively.

| Process | Generator |
|--|---------------------------------|
| ggF, VBF | POWHEG [<u>57, 58</u>]+PYTHIA |
| $WH, ZH, t\bar{t}H$ | PYTHIA |
| W+jets, Z/γ^* +jets | ALPGEN [59]+HERWIG |
| tī, tW, tb | MC@NLO [60]+HERWIG |
| tqb | AcerMC [61]+PYTHIA |
| $q\bar{q} \rightarrow WW$ | MC@NLO+HERWIG |
| $gg \rightarrow WW$ | gg2WW [62]+HERWIG |
| $q\bar{q} \rightarrow ZZ$ | POWHEG [63]+PYTHIA |
| $gg \rightarrow ZZ$ | gg2ZZ [64]+HERWIG |
| WZ | MadGraph+PYTHIA, HERWIG |
| $W\gamma$ +jets | ALPGEN+HERWIG |
| $W\gamma^*$ [65] | MadGraph+PYTHIA |
| $q\bar{q}/gg \rightarrow \gamma\gamma$ | SHERPA |



How to estimated background

- Background estimated by running a Monte Carlo simulation
- Simulated a poisson distributed energy distribution over the quark and calculated the outcome of a collision

Simulations were also experimental validated first



Reconstruction of event

- Approximately 20 collisions at one time
- Indentify those different collisions
- Make use of momentum, energy and charge conservation and the laws of particle physics



Missing transverse momenta

Due to neutrino losses

 Neutrinos from decay channels: Leads to broad distribution of higgs mass peak



Detection ZZ->4I decay

 Data is measured, signal is expected value for Higgs





Detection di-photon decay

Relative strong signal

Rescaled, why ?







Combined data CMS

Overview of excess events of the different channels





Combined data CMS

- ZZ-> 4I and diphoton channels show a clear excessive amount of event around the mass of 125 GeV
- The other channels show to much background compared to signal



Conclusion experiment

- In 2011 at 7 Tev 4.6–4.8 fb^{-1,} a mass of 124–126 GeV with significances of 2.9 and 3.1 ATLAS and CMS
- Combing this with data from 2012 running at 8 Tev and 5.8–5.9 fb⁻¹

A Boson is found at

- Atlas: 126.0 ± 0.4 (stat) ± 0.4 (sys) GeV significances 5.1 σ
- CMS: 125.3 ± 0.4 (stat) ± 0.5 (sys) GeV. significicances 4.6 σ

Is it a Higgs particle?



How to verify the SM Higgs

An investigation into the properties the SM demands for the Higgs particle



SM Higgs

- Couples to all particles with mass
- Spin-0
- Parity +



SM couplings

- Five Higgs decay channels: γγ, WW^(*), Z Z^(*), τ⁺τ⁻, bb-bar
- Determine signal strength for all these. Hard for some:
- $WW^{(*)} \rightarrow IvIv$: missing p_T from neutrinos
- T⁺T⁻: decays in many particles, also missing p_T
- bb-bar: much SM noise and big uncertainty due to high energetic jets



- Differentiating between Higgs production modes helps to bypass the SM noise
- ggF, gluon-gluon fusion: gg —-т loop--> H
- VBF, vector boson fusion: WW, ZZ -> H
- VH, associated production: W, Z -> H + W, Z



SM: Branching ratios

April 2013 CMS preliminary results





Spin

- Using observed decays, spin can be determined by exclusion
- Spin-0 can also be concluded From isotropic higgs decay
 *full knowledge of decay
 Kinematics and production is required
- spin of decay elementary particles:



Spin Scenarios



Observing fermionic decay modes will rule out spin-2 and therefore will prove spin-0 scenario



Spin Scenarios



- b quark decay not sufficient
- H -> T⁺T⁻ will prove conclusive
- Currently, data of H -> T⁺T⁻ channel is still inconclusive



ATLAS note

- ATLAS note 16 april 2013
- Spin and parity can be determined by reconstructing kinematics in channels
 - H -> <u>ZZ</u>^(*) -> 4|,
 - H -> yy,
 - $\blacksquare H \rightarrow WW^{(*)} \rightarrow |V|V$
- Spin-parity hypotheses J^p: 0⁺ compared to other scenarios
- The data strongly favour the $J^p = 0^+$ hypothesis
- Although $J^p = 0^+$ is likely, results are not conclusive



concluding

- Exact coupling of new boson to other particles must be further determined
- Spin-parity seems to be in accordance to SM, but too early to tell
- LHC operation will resume in 2015, reaching 14 TeV CME
- Future data will prove affirm Higgs boson or otherwise investigate any aspects of EW symmetry breaking



Why beyond the standard model

Higgs mass not predicted in SM $m_H = \sqrt{2\lambda v}$ Hierachy problem/fine tuning of the Higgs mass Higgs vev on comological constant

Number of families and higgs implications

- Charge quantization and unconnected lepton quark content
- Neutrino oscillations, right handed neutrino? Dark matter
- Matter antimatter ass
- Matter antimatter assymetry
- Fermion masses and mixing angles
- Gauge coupling unification



Hierachy problem

- The standard model has a drawback.
- Introduce an energy cut off scale Λ, beyond this the standard model is not more valid.
- $\Lambda \rightarrow \infty$ is some sense not really a problem.
- But this is where the hierachy problem comes in.



Hierachy problem

- The Higgs mass is determined by it's propagator
- The propgator is a sum of the tree mass and quantum corrections in the form of one loop diagrams

• So
$$m_h^2 \sim m_{tree}^2$$
 + (quantum corrections)²

This tree mass is a free parameter but must be chosen large to cancel the main quantum correction loop. The main quantum correction contributions to the Higgs mass





Quadratic divergence

- $\hfill \hfill \hfill$
- with $\Lambda \sim 10 TeV$ the main contributions are

$$-\frac{3}{8\pi^2}\lambda_t^2\Lambda^2 \sim -(2TeV)^2 \text{ from the top loop,}$$
$$\frac{1}{16\pi^2}g^2\Lambda^2 \sim (700\,GeV)^2 \text{ from the gauge loop, and}$$
$$\frac{1}{16\pi^2}\lambda^2\Lambda^2 \sim (500\,GeV)^2 \text{ from the Higgs loop.}$$

- The free parameters $\lambda_t\,\lambda$ and g determine the precise values of the contributions.



Higgs mass is "unnaturally" small

The following graph show estimates of the ratios between the loop corrections.





Fine tuning

- So we see that the fine tuning of the paramters λ_t , λ and g' must be extremely precise, about 1 part in 100
- Setting $\Lambda \sim 1 TeV$ reduces the magnitude of the corrections to the same scale as the Higgs boson and hence there is no hierachy or fine tuning problem.
- This would however mean there should be some new physics beyond the standard model. Any such physics would arise at a energy scale above Λ



Vacuum energy density

• The higgs vev impies is a 10⁵⁴ order too large?

$$V \min = V(v) = \frac{-1}{8} m_h^2 v^2$$
$$\Lambda_h = \frac{1}{8} m_h^2 v^2 = 10^8 GeV^4$$
$$\Omega_\Lambda = 10^{-46} GeV^4$$

Beyond the standard model physics saving hierarchy

 We will discuss theories which will either completely solve the hierarchy problem or shift A to a higher energy.

The most well known and studied beyond the standard model (BSP) is supersymmetry, which takes care of the hierarchy on any energy scale.

• The little Higgs model solves the hierarchy problem on up to scales of

Susy



- Spin opposide partners & spartners
- MSSM Minimal SuSy Model is the minimal extension of SM
- N=1; Bosons and fermions have 1 superpartner from opposite sector

- In unbroken susy; superpartners have equal mass.
- Quantum loops of supersymmetric partners have an opposite sign.
- These means that the hierarchy problem is solved.
- However this would also imply that the Higgs mass is zero
- No Susy particles found yet.

Susy breaking

- Susy as a broken symmetry ~1TeV in the Early universe
- For every loop correction diagram in SM we can introduce a SUSY



- Broken symmetry; non equal masses of the superpartners.
- Almost 100% cancellation. Higgs obtains natural small mass
- Hierarchy problem solved...?



Particles in Susy L_{SM}

5 fermion (spin $\frac{1}{2}$) representations Q_L(3,2), u_R(3,1), d_R(3,1), L_L(1,2), e_R(1,1) 12 massless gauge boson (spin 1) fields 1B, 3W, 8G.

In susy a supersymmetric partner of higgs fields (complex duplet) introduced: 8 dof.

After spontaneous breaking with Higgs mechanism:

- W⁺ ,W⁻,Z⁰ massive (3 dof)
- γ,8G massless

5 massive scalar higgs particles!h⁰, H⁰CP even higgs bosonsA⁰CP oddH⁺, H⁻.Charged higgs

Particles in Susy L_{susy}

5 'sfermion' (spin 1) representations 12 gauge (spin ½) fields: Bino, Wino⁺, Wino⁻, Wino⁰ and 8 Gluinos.

The 2 higgs fields introduce again 8 dof. After spontaneous symmetry breaking:

| 1 Bino | massless | В |
|-------------|----------|---|
| 3 Winos | massive | W+ ,W-,W0 |
| 5 Higgsinos | massive | <u>h</u> ⁰, <u>H</u> ⁰, <u>A</u> ⁰, <u>H</u> ⁺, <u>H</u> ⁻. |
| 8 Gluinos | massless | G |

The Bino, neutral Wino and neutral Higgsinos mix to create 4 Neutralinos $\chi_{1,2,3,4}$

The charged Winos and charged Higgsinos mix to create 4 Charginos $x_1^+, x_1^-, x_2^+, x_2^-$

The 8 Gluinos remain massless.




In R-parity conserving models; stable neutralino!



Higgs mass in MSSM

MSSM Higgs Decoupling limit

[

- $m_A >> m_Z$. 1 light higgs scalar particle h^0 $m \sim M_{Hsm}$
- The other 4 higgs particles have a mass ~1TeV: discovery difficult

$$m_{h^{0},H^{0}}^{2} = \frac{1}{2} \left(m_{A^{0}}^{2} + m_{Z}^{2} \mp \sqrt{(m_{A^{0}}^{2} + m_{Z}^{2})^{2} - 4m_{Z}^{2}m_{A^{0}}^{2}\cos^{2}2\beta} \right)$$

$$M_{h}^{2} \stackrel{M_{A} \gg M_{Z}}{\approx} M_{Z}^{2}\cos^{2}2\beta + \frac{3m_{t}^{4}}{2\pi^{2}v^{2}} \left[\log \frac{M_{S}^{2}}{m_{t}^{2}} + \frac{X_{t}^{2}}{M_{S}^{2}} \left(1 - \frac{X_{t}^{2}}{12M_{S}^{2}} \right) \right].$$

$$m_{h}^{2} \stackrel{M_{A} \gg M_{Z}}{\approx} M_{Z}^{2}\cos^{2}2\beta + \frac{3m_{t}^{4}}{2\pi^{2}v^{2}} \left[\log \frac{M_{S}^{2}}{m_{t}^{2}} + \frac{X_{t}^{2}}{M_{S}^{2}} \left(1 - \frac{X_{t}^{2}}{12M_{S}^{2}} \right) \right].$$

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Questions?



Little Higgs

- A viable model is the Little Higgs
- The little Higgs theory cancells the loop corrections to a higher energy scale $\Lambda \sim 10 TeV$

S

Backup slides





Notice style $\sqrt{2\lambda}v$

The higgs propagator receives loop corrections from gauge bosons, higgs self interactions For large Mh SI dominate at relative low energies.

m_h < 700 GeV down (soft limit) Perbutation theory breaks



Higgs mass

The requirement that λ remains positive in order to keep a global minima in the higgs quartic polynomial for the potential V= $\mu^2 \phi^2 + \lambda^2 \phi^4$, up to the GUT energy scale Λ =10¹⁶ GeV puts a lower limit on λ and m_h,

 $m_h > 135 \text{ GeV}$ Vacuum stability $\lambda > 0$

Thick groups ling constant λ depends like all gauge coupling constants on energy, $d\lambda / dt = \beta_{\lambda}$ with $t = \ln(Q^2)$. The evolution of the β function sets a limit on the higgs mass, if we require that $\lambda < \infty$ up to the GUT scale $\Lambda = 10^{16}$ GeV,

 $m_h < 160 \text{ GeV}$ Landau pole $\lambda < \infty$

Hh-graviton-hh needed!!









Planck 10/19

Baryogenesis? Matter/antimatter assymetry GUT 10^14 Mx 10¹⁴GeV Gut breaking. SU5->SU3 xSU2. Quarks en leptons. Susy breaking 1TeV Mass difference. Sarticles not observed Elektroweak breaking Mh~246GeV Strong en SU2xU1 apart Decay to particles. Reheating ?Inflation? Quark/gluon plasma filles universe Hadron p,n Lepton Photon Nucleosynthesis He4 Recombination Free streaming. CMB Acoustic oscc.

Stars, Galaxies, Clusters

$$\begin{split} (D_{\mu}\phi) &= \frac{1}{\sqrt{2}} \left[ig\frac{1}{2} \vec{\tau} \cdot \vec{W_{\mu}} + ig'\frac{1}{2}YB_{\mu} \right] \begin{pmatrix} 0 \\ v \end{pmatrix} \\ &= \frac{i}{\sqrt{8}} \left[g(\tau_{1}W_{1} + \tau_{2}W_{2} + \tau_{3}W_{3}) + g'YB_{\mu} \right] \begin{pmatrix} 0 \\ v \end{pmatrix} \\ &= \frac{i}{\sqrt{8}} \left[g\left(\begin{pmatrix} 0 \\ W_{1} & 0 \end{pmatrix} + \begin{pmatrix} 0 \\ iW_{2} & -iW_{2} \end{pmatrix} + \begin{pmatrix} W_{3} & 0 \\ 0 & -W_{3} \end{pmatrix} \right) + g'\begin{pmatrix} Y_{\phi_{0}}B_{\mu} & 0 \\ 0 & Y_{\phi_{0}}B_{\mu} \end{pmatrix} \right] \begin{pmatrix} 0 \\ v \end{pmatrix} \\ &= \frac{i}{\sqrt{8}} \left(\begin{array}{c} gW_{3} + g'Y_{\phi_{0}}B_{\mu} & g(W_{1} - iW_{2}) \\ g(W_{1} + iW_{2}) & -gW_{3} + g'Y_{\phi_{0}}B_{\mu} \end{array} \right) \begin{pmatrix} 0 \\ v \end{pmatrix} \\ &= \frac{iv}{\sqrt{8}} \left(\begin{array}{c} g(W_{1} - iW_{2}) \\ -gW_{3} + g'Y_{\phi_{0}}B_{\mu} \end{array} \right) \end{split}$$

We can then also easily compute $(D^{\mu}\phi)^{\dagger}$: $(D^{\mu}\phi)^{\dagger} = -\frac{iv}{\sqrt{8}} \left(g(W_1 + iW_2), (-gW_3 + g'Y_{\phi_0}B_{\mu}) \right)$ and we get the following expression for the kinetic part of the Lagrangian:

$$(D^{\mu}\phi)^{\dagger}(D_{\mu}\phi) = \frac{1}{8}v^{2}\left[g^{2}(W_{1}^{2}+W_{2}^{2}) + (-gW_{3}+g'Y_{\phi_{0}}B_{\mu})^{2}\right]$$
(7)



Couplings to higgs $h \to f\overline{f}$



$$M^{2} = \left(\frac{m_{f}}{v}\right)^{2} \left[-4p1p2 - 4m_{f}^{2}\right]$$

$$M^{2} = \left(\frac{m_{f}}{v}\right)^{2} \left[2m_{h}^{2} - 8m_{f}^{2}\right] = \left(\frac{m_{f}}{v}\right)^{2} \left[1 - x\right]N_{c}$$

$$d\Gamma = (\frac{m_f}{v})^2 \frac{m_h N_c}{8\pi} [1 - x]^{\frac{3}{2}}$$



$$\Gamma_{H\to\gamma\gamma} = \frac{\alpha^2 g^2 m_H^3}{1024\pi^3 m_W^2} \left| \sum_i N_c e_i^2 F_i \right|$$

$$\Gamma_{H \to gg} = \frac{\alpha_s^2 g^2 m_H^3}{512\pi^3 m_W^2} \left| \sum_i F_i \right|$$