The Electronic News Net of the
SIAM Activity Group on Orthogonal Polynomials and Special Functions

http://math.nist.gov/opsf

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Editors:
Howard S. Cohl    howard.cohl@nist.gov
Kerstin Jordaan   kerstin.jordaan@up.ac.za

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Calendar of Events:

June 1–5, 2015
13th International Symposium on Orthogonal Polynomials, Special Functions and Applications (OPSFA13), NIST, Gaithersburg, Maryland, USA
http://www.siam.org/meetings/opsfa13

June 7–11, 2015
“Asymptotics in integrable systems, random matrices and random processes and universality”, in honour of Percy Deift’s 70th birthday,
Centre de Recherches Mathématiques, Montreal, Canada
http://www.crm.umontreal.ca/2015/Deift15/index_e.php

June 8–12, 2015
V Iberoamerican Workshop on Orthogonal Polynomials, Mexico City, Mexico
June 10–13, 2015  
AMS–EMS–SPM International meeting, with a special session on Orthogonal Polynomials and Integrable Systems, Porto, Portugal  
http://aep–math2015.spm.pt

June 15–18, 2015  
Progress on Difference Equations, Covilhã, Portugal  
http://www.pode2015.ubi.pt

15 June–10 July, 2015  
SERB (DST) – sponsored 12th SERB School on Matrix Methods & Fractional Calculus, Peechi Campus, KFRI, Peechi –680653, Kerala, India  
Contact mathai@math.mcgill.ca for more information

August 9–14, 2015  
Orthogonal and Multiple Orthogonal Polynomials, Oaxaca, Mexico  
http://www.birs.ca/events/2015/5–day–workshops/15w5022

August 10–14, 2015  
ICIAM 2015 (International Congress on Industrial and Applied Mathematics), Beijing, China  
http://www.iciam2015.cn

August 26–28, 2015  
Symposium “The Real World is Complex” in honour of Christian Berg, in Copenhagen, Denmark  
http://www.math.ku.dk/~henrikp/cb

September 10–12, 2015  
XIVth Annual Conference (ICSFA 2015) of Society for Special Functions & their Applications (SSFA), Amity University, Noida, India  
http://www.ssfaindia.webs.com/conf.htm

September 28–30, 2015  
International Conference on Analysis, Applications and Computations, In Memory of Lee Lorch, Fields Institute, Toronto, Canada  
http://www.fields.utoronto.ca/programs/scientific/15–16/analysisapplications

October 4–30, 2015  
International Workshop and Latin–American School on Foundations of Complexity, Nonadditive Entropies and Nonextensive Statistical Mechanics, Rio de Janeiro, Brazil  
http://www.cbpf.br/~complex

June 27 – July 1, 2016  
Abecederian of SIDE (ASIDE) 12 Summer School, Centre de Recherches mathématiques, Université de Montréal, Montréal, Quebec, Canada  
July 3–9, 2016
Symmetries and Integrability of Difference Equations 12,
Hôtel Le Chanteclerc, Saint Adèle, Québec, Canada

July 11–15, 2016
OPSF-S6 Summer School on Orthogonal Polynomials and Special Functions,
American University, Washington D.C., USA
https://wis.kuleuven.be/events/OPSFA

Topic #1  _______ OP – SF Net 22.3  _______ May 15, 2015

From: Walter Van Assche (walter@wis.kuleuven.be)
Subject: CALL for OPSFA–14 (Deadline May 31, 2015)

The Steering Committee of the international symposia “Orthogonal Polynomials, Special Functions and Applications” has opened a call for the organization of the next international symposium on “Orthogonal Polynomials, Special Functions and Applications” (OPSFA–14), to be held preferably in 2017. Please inform Walter Van Assche (walter@wis.kuleuven.be) if you are willing to organize OPSFA–14.

The deadline is May 31, 2015. Please provide:

• name of the contact person;
• place where the conference will be organized; and a
• suggestion of the date.

All proposals will be evaluated by the steering committee and the final decision will be announced at the upcoming OPSFA–13 meeting in Gaithersburg, USA (June 1–5, 2015).

The Steering Committee for OPSFA consists of 3 local organizers of the past 5 OPSFA meetings and a representative of the SIAM Activity Group “Orthogonal Polynomials and Special Functions” (not necessarily the chair). This Steering Committee was founded during the OPSFA–11 meeting in Leganés, Spain, in 2011. Its main task is to coordinate the international meetings in the OPSFA community, such as the biannual international symposium and summer schools. Presently the Steering Committee consists of:

Walter Van Assche (SIAG chair and OPSFA–10)
Guillermo López Lagomasino (OPSFA–11)
Mohamed Jalel Atia (OPSFA–12)
Diego Dominici (SIAG program director)

See also: https://wis.kuleuven.be/events/OPSFA/Call.
In the first week of March (March 3–6, 2015), a conference on “Representation Theory, Special Functions and Painlevé Equations” took place at the Research Institute of Mathematical Sciences (RIMS) of Kyoto University in Kyoto, Japan. This event, held in honor of Professor Masatoshi Noumi of Kobe University on the occasion of his 60th birthday celebration, was organized by H. Konno, Y. Masuda, M.–H. Saito, H. Sakai, J. Shiraishi, T. Suzuki and Y. Yamada. The themes of the meeting, nicely summarized in its title, were around a selection of areas where Noumi–san has made fundamental contributions: symmetric functions (Macdonald polynomials and the likes), hypergeometric transformation and summation formulas, Painlevé transcendents, elliptic integrable systems and elliptic hyper geometry, and representation theory underlying these special functions.

The conference program consisted of 60 minute talks separated by generous breaks of at least 30 minutes. On the opening day and on the closing day, only 3 afternoon and 2 morning talks were scheduled, respectively, while on the remaining two full days, the schedule consisted of 5 talks. Since the range of topics was wide, most speakers did a nice unselfish job by starting with a helpful survey of the field before thrusting towards the latest state of the art developments. This way, even for a participant mastering only a small portion of Noumi–san’s research interests (like myself), there was a lot to be captured also from talks on topics which one is less familiar with.

One of the highlights of the conference was the talk of Noumi–san himself “Special functions arising from elliptic integrable systems,” which took the audience on a fascinating tour connecting elliptic hypergeometric series and integrals, elliptic Painlevé equations, and elliptic integrable systems. Other presentations included: Yasushi Kajihara: Families of transformations for bilinear sum of (basic) hypergeometric series and multivariate generalizations; Tom Koornwinder: Some remarks about Koornwinder polynomials; Simon Ruijsenaars: Quantum integrable systems of elliptic Calogero–Moser type; Jasper V. Stokman: From Noumi’s representation to elliptic K–matrices; Frank W. Nijhoff: On elliptic Lax pairs and isomonodromic deformation problems for integrable lattice systems; Nalini Joshi: Elliptic asymptotics for discrete Painlevé equations; Kenji Kajiwara: Integrable discrete deformations of discrete curves: geometry and solitons, old and new; Philip Boalch: Non–perturbative symplectic manifolds and non–commutative algebras; Marta Mazzocco: Painlevé equations and q–Askey scheme; Tôru Umeda: Remarks on the Capelli identities for reducible modules; Anatol N. Kirillov: Plactic algebra, Cauchy kernels and plane partitions; Katsuhisa Mimachi: Monodromy representations associated with the generalized hypergeometric function \( \binom{n+1}{n}F_n \); Vyacheslav P. Spiridonov: Elliptic hypergeometric functions and superconformal indices; Jan Felipe van Diejen: Branching formula for Macdonald–Koornwinder polynomials. (Freak detail: the participants of the Japanese and Dutch nationalities each accounted for one third of the lecture program.)

Since the scientific program ended each day at 17:00 at the latest, the conference participants had plenty of opportunities to explore the many touristic attractions of Kyoto as well. While on Thursday evening, folks met at the impressive Funatsura Japanese Inn for Noumi–san’s after–lecture birthday party.

The smooth organization, top location, and many inspiring talks, certainly made this pleasant conference into a memorable one.

In the past there have been great relations between mathematics and physics. Mathematical formalism entered the development of theoretical physics or problems arising from physics encouraged developments in mathematics. A. M. Mathai’s 80th birthday is a welcome opportunity to celebrate his contributions to the theory of special functions of mathematical physics and to note the current stormy development of the mathematics and statistics of fractional calculus and its surprising applications in physics and beyond published in a special issue Special Functions: Fractional Calculus and the Pathway for Entropy Dedicated to Professor Dr. A. M. Mathai at the occasion of his 80th Birthday of Axioms.

One of Mathai’s early applications of the theory of special functions in (astro)physics was related to the prospective resolution of what is known in the literature as the ‘solar neutrino problem’. This problem was a major discrepancy between measurements of the numbers of solar neutrinos streaming through the Earth and theoretical models of the solar interior, lasting from the mid–1960s to about 2002. The discrepancy has since been resolved by new understanding of neutrino physics, requiring a modification of the standard model of particle physics – specifically, neutrino oscillations. Essentially, as neutrinos have mass, they can change from the type that had been expected to be produced in the Sun’s interior into two types that would not be caught by the detectors in use at the time. Mathai’s contributions to the resolution of this problem were discussed with R. Davis Jr. who received the 2002 Nobel Prize in physics for the resolution of the solar neutrino problem. Related to this problem, in the 1980s, Mathai made important contributions to the closed–form representation of solar thermonuclear reaction rates in terms of Meijer’s G–function which are a fundament of nuclear astrophysics. In 1983, W. A. Fowler received the Nobel Prize in physics for his leading developments in the field of nuclear astrophysics. Mathai’s mathematics and statistics for solar neutrinos and solar nuclear astrophysics remain to be fundamental contributions to both fields of on–going research.

The two dominant examples of interaction between mathematics and physics in the twentieth century are Riemannian geometry in general relativity and the impact of quantum mechanics on development of functional analysis. Einstein finalized general relativity in 1915, while quantum field theory has been an open frontier since its foundation in 1927 by Dirac based on Heisenberg’s and Schroedinger’s physics. This happened almost 100 years ago. For the next fifty years there was not much interaction between theoretical...
physics and mathematics. Mathematics turned to more abstract accomplishments, while quantum field theory was formulated in a rather formal way.

There are two fundamental theories in twentieth century physics: general relativity and quantum field theory. General relativity describes gravitational forces on the scale of the macrocosmos, while quantum field theory describes the interaction of elementary particles, electromagnetism, strong and weak forces at the scale of the microcosmos. There remains to be an inconsistency between the two theories. The formal quantization of general relativity leads to infinite formulas. Einstein invented general relativity to resolve an inconsistency between special relativity and Newtonian gravity. Quantum field theory was invented to reconcile Maxwell's electromagnetism and special relativity with non-relativistic quantum mechanics. But there were two basically different approaches. In Einstein's "thought experiments", which led to the discovery of general relativity, the logical framework was first. Then in Riemannian geometry of general relativity, the correct mathematical framework was found. In the development of quantum field theory on the other hand, there was no a priori conceptual basis; experimental clues played an important role, but there was no mathematical model. To date string theory is progressing in the pursuit to a formal quantization of general relativity: if accomplished it might be called the first revolution in physics in the twenty first century.

A second revolution in the making in the twenty first century might be the development of statistical mechanics beyond Boltzmann and Gibbs, taking into account the need for a physical theory for stochastic processes in non-equilibrium systems. Indications are there that the mathematics for such a theory is given with fractional calculus and Fox' H-function playing a central role in the solutions of stochastic fractional differential equations of the type of Liouville, master, Fokker-Planck, Langevin, and reaction-diffusion. However, the physical interpretation of fractional time and space derivatives and integrals has not been discovered yet and a prospective physical theory based on a "Schrodinger equation for thermodynamics", as referred to by Prigogine even if he surely had in mind a master equation, has not been discovered. Mathai's research programme from the 1970s, as outlined in three monographs, all published in the short time interval between 1875 and 1978,

![Books](image1.png)

![Books](image2.png)

![Books](image3.png)

does address in terms of mathematics and statistics some of the open issues for the second revolution in physics in the twenty first century: The monograph Mathai/Rathie contains a generalization of Shannon's information entropy that also supports Tsallis' successful but still hotly debated generalization of Boltzmann–Gibbs entropy for non-extensive statistical mechanics and the maximum entropy framework for non-exponential distributions as alluded to in the Mathai/Pederzoli monograph. Today the Mathai/Saxena
monograph on Fox’ H-function is considered essential for many mathematicians and statisticians as the “bible” for the application of generalized hypergeometric functions in the natural sciences and central to deriving closed-form solutions of fractional master, Fokker-Planck, Langevin, and reaction-diffusion equations. Mathai is still working on the analysis of data and problems from solar neutrino observatories, operated by international teams of scientists in the US, Japan, and Europe to unfold the mystery that the solar neutrino flux seems to indicate non-Gaussian statistics showing harmonic modulation that might be modeled by a fractional dissipative first-order stochastic differential equation. This issue is not yet settled neither in (astro)physics nor in mathematics and statistics.


Topic #4  OP – SF Net 22.3  May 15, 2015

From: Howard Cohl (howard.cohl@nist.gov)
Subject: Erratum to “Bessel Functions” (2014) by K. B. M. Nambudiripad

The following errors and misprints have been detected in the monograph of Nambudiripad (2014) Bessel Functions, Alpha Science International Ltd., Oxford, U.K.¹

Comments

• p. 2.4, (v), p. A.1, (iv). The outdated notation \( \Pi(n) \) should be replaced with \( n! \).

• p. 6.4, (6.6) & p. A.8. The term

\[
\left[ 1 + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{m} + \frac{1}{2} + \frac{1}{3} + \cdots + \frac{1}{n+m} \right]
\]


in the infinite series expansion of \( K_n(x) \) is incorrect. It’s missing a sum contribution of 1 and is meaningless for \( m = 0 \). One should replace this term with a sum of harmonic numbers \( H_m + H_{n+m} \), where \( H_0 := 0 \) and \( H_p := \sum_{k=0}^{p} \frac{1}{k} \) for \( p \geq 1 \).

• p. 6.4, Section 6.1.2. In the string of 4 equalities evaluating \( J_\nu(ix) \), the third and fourth equalities are not equal to \( J_\nu(ix) \). However it is true (and follows from the derivation) that \( I_\nu(x) = i^{-\nu} J_\nu(ix) \).

• p. 6.7, (6.12). Because of the previous string of sign errors in this section (see below), and a missing factor of two, one should have

\[
I_\nu'(r) = \frac{1}{4} [I_{\nu-2}(r) + I_\nu] + \frac{1}{4} [I_{\nu}(r) + I_{\nu+2}(r)] = \frac{1}{4} [I_{\nu-2}(r) + 2I_\nu(r) + I_{\nu+2}(r)].
\]

• p. 7.5, (7.13). It is not true that \(-i\) can be represented as \((\sqrt{i})^2\).

• p. 7.5, between (7.16) & (7.17). The statement \( i^{1/2} = (\sqrt{-1})^{1/2} = i^{3/2} \) is not true. Furthermore, \( i^{1/2} \) does not equal \( i^{3/2} \).

¹Errata for this book is not intended to imply recommendation or lack thereof by the National Institute of Standards and Technology. Opinions expressed are those of the author.
• p. 7.6, line –1. The parenthetical sentence “(The order, ν, is itself a fraction, in general.)” is incorrect.

• p. 9.13, line –2. Remove ‘.’ at end of line.


• p. C.{2,4,5,6,7,8}. The author gives formulas for x > {15.9, 15.9, {15.9, 10}, 10, 10, 10} in Appendix C, when entries are not given in this range of x. There is no way to compare these formulae with numerical values. Furthermore, there is no discussion on their numerical comparison. No motivation is explained as to why these formulas are inserted or where they originated from. Since these are approximate formulas, the reader does not understand why > is sometimes used and ≥ used other times.

• p. C.5, Table C.9, Entry (x = 0, Y1(x)). Remove typographical error “box”.

### Replacements

<table>
<thead>
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<th>For</th>
<th>Read</th>
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<td>p. 2.3, Fig. 2.1.</td>
<td>J0, J1, J2, J3</td>
<td>J1, J2, J3, J4</td>
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<td>p. 2.5, Table 2.1.</td>
<td>J0x</td>
<td>J0(x)</td>
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<td>p. 3.7, (3.7).</td>
<td>0</td>
<td>0</td>
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<td>H0(1), H0(2)</td>
<td>H0(1)(x), H0(2)(x)</td>
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<td>p. 4.2, line 4.</td>
<td>Γ(x)</td>
<td>xΓ(x)</td>
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<tr>
<td>p. 4.6, line 2.</td>
<td>√2Γ(½)</td>
<td>√2Γ(½)</td>
</tr>
<tr>
<td>p. 4.3–4.4, (4.4).</td>
<td>(n – m + 1)!</td>
<td>(n – m – 1)!</td>
</tr>
<tr>
<td>p. 4.3–4.4, (4.4).</td>
<td>(-1)m</td>
<td>½(-1)m</td>
</tr>
<tr>
<td>p. 4.6, line 3.</td>
<td>√2√π</td>
<td>√2√π</td>
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<td>p. 5.2, eq. 2.</td>
<td>ei, ej</td>
<td>ei, ej</td>
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<tr>
<td>p. 5.2, eq. 3.</td>
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<td>ei, ej</td>
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<tr>
<td>p. 5.3.</td>
<td>i = 0</td>
<td>i = 1</td>
</tr>
<tr>
<td>p. 5.3, line –1.</td>
<td>≠ 0 if m = n.</td>
<td>= 0 if m = n.</td>
</tr>
<tr>
<td>p. 5.4, Section 5.1.4.</td>
<td>ϕ1, ϕ2, ϕ3,…</td>
<td>ϕ0, ϕ1, ϕ2,…</td>
</tr>
<tr>
<td>p. 5.4, Section 5.1.4.</td>
<td>⟨ϕm(x)ϕn(x)⟩</td>
<td>⟨ϕm(x), ϕn(x)⟩</td>
</tr>
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<td>p. 5.4, Section 5.1.4.</td>
<td>if m ≠ n ≠ 0 if m = n.</td>
<td>if m ≠ n and ≠ 0 if m = n.</td>
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<tr>
<td>p. 5.12.</td>
<td>R(ν) &gt; –1</td>
<td>Re(ν) &gt; –1</td>
</tr>
<tr>
<td>p. 5.17, Line –4.</td>
<td>cm</td>
<td>cm</td>
</tr>
<tr>
<td>p. 5.21, Line 2.</td>
<td>xi</td>
<td>ξ</td>
</tr>
<tr>
<td>p. 6.3, Fig. 6.3.</td>
<td>I2(x) in lower right-hand side</td>
<td>I3(x)</td>
</tr>
<tr>
<td>p. 6.4, (6.6).</td>
<td>(π/2)n+m</td>
<td>(x/2)n+2m</td>
</tr>
<tr>
<td>p. 6.6, (6.8).</td>
<td>–</td>
<td>+=</td>
</tr>
<tr>
<td>p. 6.6, Section 6.1.4, eq. 1.</td>
<td>–</td>
<td>+=</td>
</tr>
<tr>
<td>p. 6.6, (6.9)–(6.11).</td>
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<td>+=</td>
</tr>
<tr>
<td>p. 6.8, line 2.</td>
<td>m = 0</td>
<td>m = 1</td>
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</table>
p. 6.8.

p. 6.8, line -1.

p. 6.9, eq. 2.


p. 7.1, (7.2).

p. 7.5, between (7.13) & (7.14).

p. 7.5, between (7.14) & (7.15).

p. 7.6.

p. 7.6, eq. 4.

p. 8.19.

p. 8.19, Fig. 8.3.

p. 9.12, line 7.

p. 9.12, line -7.

p. 9.18, Fig. 9.7.

p. 9.12, line 7. BesselJ BesselJ

p. 8.19, Fig. 8.3. Jz J


p. 6.9, eq. 2.

p. 6.8.

p. 7.5, between (7.13) & (7.15).

p. 7.5, between (7.14) & (7.15).

p. 10.27, eq. -1.

p. 10.28, eq. -2.

p. 10.24, eq. -1.

p. 10.28, Orthogonality.

p. 10.28, eq. -2.

p. 10.28, eq. -1, \(a_n, n \geq 1\).

p. 10.29. eq. -2.

p. 10.29. eq. -1, \(a_n\).

p. A.1, (iii).

p. A.1, (ii).


p. A.2, (x).

p. A.3, Fig. A.1.


p. A.4, eq. 2.


p. A.5.

p. A.5, (iii).

p. A.5.

p. A.5.

p. A.8, eq. 3.

p. A.8, eq. 5.

\[
\frac{d}{dr} \left[ r^{-\nu} I_\nu(r) \right] = -r^{-\nu} I_{\nu+1}(r)
\]

\[
e^{-x} \sqrt{2\pi x} (n = 0, 1, 2, \ldots)
\]

\[
I_0(\alpha a)
\]

\[
(-1)^{1/2} \text{ or } \sqrt{-i}
\]

\[
(-i)^{1/2} \text{ or } \sqrt{i}
\]

\[
i^{3m} = -1 \text{ for } m = 1, 5, 9, \ldots
\]

\[
i^{3m} = -i \text{ for } m = 2, 6, 10, \ldots
\]

\[
2l + i
\]

\[
d \left[ \frac{\omega \mu}{\rho} \right]^{-1/2}
\]

\[
d \left[ \frac{\omega \mu}{\rho} \right]^{-1/2}
\]

\[
J_z
\]

\[
BesselJ
\]

\[
x^2 e^x
\]

\[
y = y(t) = t^2
\]

\[
y \left[ x(t) \right] = \frac{dy_1}{dt}
\]

\[
\frac{dy_1}{dt}
\]

\[
eigenvalues\text{ are}
\]

\[
K_n(x) \approx \frac{e^{-x}}{\sqrt{2\pi x}}
\]

\[
a_n P_n
\]

\[
a_n H_n
\]

\[
T_n
\]

\[
a_n T_n
\]

\[
f(x)
\]

\[
a_n U_n
\]

\[
f(x)
\]

\[
J_n
\]

\[
J(0)
\]

\[
J_n, J_1, J_2, J_3
\]

\[
(-1)^m
\]

\[
n \rightarrow \infty
\]

\[
\sin \nu x
\]

\[
Y(x)
\]

\[
\text{arguments } x
\]

\[
H_0^2(x)
\]

\[
H_{\nu}^1(x) = J_\nu(x) + iY_\nu(x)
\]

\[
\left( \frac{x}{2} \right)^{n+m} (m)!
\]

\[
K_n(x)
\]

\[
J_{\nu}(0)
\]

\[
J_{-\nu}(x)
\]

\[
J_1, J_2, J_3, J_4
\]

\[
(-1)^m \frac{(x^2/4)^m}{(m)!^2}
\]

\[
m \rightarrow \infty
\]

\[
\sin(\nu x)
\]

\[
Y_n(x)
\]

\[
\text{arguments } x > 0
\]

\[
H_{\nu}^{(2)}(x)
\]

\[
H_{\nu}^{(1)}(x) = J_\nu(x) + iY_\nu(x)
\]

\[
\left( \frac{x}{2} \right)^{n+2m}
\]

\[
K_{\nu}(x)
\]
From: Pavel Winternitz (wintern@CRM.UMontreal.CA) and Decio Levi (levi@roma3.infn.it)
Subject: SIDE 12 and preceding Abecederian of SIDE (ASIDE) Summer School

Centre de Recherches Mathématiques (CRM), Université de Montréal, will hold SIDE 12, the twelfth in a series of biennial conferences devoted to Symmetries and Integrability of Difference Equations and related topics such as ordinary and partial difference equations, analytic difference equations, orthogonal polynomials and special functions, symmetries and reductions, difference geometry, integrable discrete systems on graphs, integrable dynamical mappings, discrete Painlevé equations, singularity confinement, algebraic entropy, complexity and growth of multivalued mapping, representations of affine Weyl groups, quantum mappings and quantum field theory on the space–time lattice and physical applications. SIDE 12 will take place at Hôtel Le Chanteclerc, Saint Adèle, Québec, Canada from July 3 through July 9, 2016.

SIDE 12 will be preceded by the Abecederian of SIDE (ASIDE) summer school for young participants (graduate students and postdoctoral fellows) which will be held at Centre de Recherches Mathématiques, Université de Montréal from June 27 through July 1, 2016. The goal of ASIDE is to gather early career researchers, post-doctoral fellows and PhD students for a week–long series of mini–courses taught by their peers. These introductory mini–courses will cover the topics represented at the SIDE meeting. The Organizing Committee for ASIDE 12 consists of:

Vincent Genest, Chair (CRM)
Ferenc Balogh (Concordia)
Rapahël Rebelo (CRM)
Bart Vlaar (Nottingham)

Joseph Lehner was born in New York City on October 29, 1912 to Louis and Rachel (Rosenblum), and died in Haverford, PA on August 5, 2013. Lehner’s scientific work was primarily concerned with automorphic forms for discontinuous groups and related number theory.

In 1964, Lehner published one of the first treatises in English on automorphic forms [3], which included both the historical beginnings of the subject as well as later developments, due especially to E. Hecke, H. Petersson, H. Rademacher, and C. L. Siegel. This book has become a classic, and has served as an introductory book to automorphic forms for many generations.

Lehner’s seminal joint paper with Oliver Atkin [1] introduced a method to study the arithmetic of modular forms which fundamentally changed the field. The idea was to collect together forms for congruence subgroups \( \Gamma_0(m) \) for all \( m \geq 1 \). For forms of \( \Gamma_0(m) \), they distinguished “oldforms,” which arise naturally from cusp forms of \( \Gamma_0(n) \) with \( n \) dividing \( m \), and “newforms,” which are forms which genuinely live in \( \Gamma_0(m) \). They pioneered the “theory of newforms,” which reduces the study of the arithmetic of modular forms for \( \Gamma_0(m) \) to that of newforms, and they studied the arithmetic of newforms in detail. The Atkin–Lehner theory of newforms was extended by T. Miyake [5] to forms for congruence subgroups \( \Gamma_1(n) \) and completed by the second author [4] for forms for all congruence subgroups of \( SL_2(\mathbb{Z}) \). The newform theory naturally led to automorphic forms and automorphic representations for \( GL_2 \) in the adelic setting, and it therefore has had a far-reaching impact in the theory of automorphic forms. To date, researchers have been extending their ideas to study newforms for orthogonal groups. The Atkin–Lehner operators introduced in their paper [1] also play a fundamental role in the study of elliptic and Shimura modular forms.

Lehner earned his BS at New York University (1938) and his MA (1939) and PhD (1941) at the University of Pennsylvania under the supervision of Hans Rademacher, whom he was later to describe as his teacher and friend. Lehner was the 6th of Rademacher’s 21 doctoral students, and the third author of this obituary is the second of Lehner’s four doctoral students.

Lehner began his academic career as an instructor at Cornell in 1941–1943. In 1943, he joined Kellex Corporation, which was involved with the design and initial operation of the K25 diffusion plant at Oak Ridge (Manhattan Project). His group, which included Manson Benedict and Elliott Montroll, developed a highly advanced mathematical theory of how a cascade of approximately four thousand stages would respond to time–dependent disturbances in its performance – whether a cascade would magnify the disturbance, leading ultimately to a disruptive or destructive surge in pressure, or whether the cascade would damp out these fluctuations as it went through successive stages. Lehner and Montroll were the principal mathematicians who consequently solved systems of time and space dependent partial differential equations, which led to an efficient method for producing U–235 at a newly constructed plant at Oak Ridge. For further information about contributions made by Lehner, nuclear engineer Manson Benedict (recipient of the National Medal of Science in 1975), and their group, consult an informative interview with Bene–
dict [2]. After three years, Lehner left Kellex to become head of the mathematics group at Hydrocarbon Research Inc.

Lehner returned briefly to academia as an Associate Professor at the University of Pennsylvania in 1949-1952, before joining Los Alamos Scientific Laboratory for five years, followed by two additional years as a consultant. At Los Alamos, he further worked on the Manhattan Project, developing theories of diffusion cascades and neutron transport. In 1957, he returned to academic pursuits to become Professor at Michigan State University for six years, which were followed by nine years at the University of Maryland. His last position was as Mellon Professor at the University of Pittsburgh from 1972 to 1980.

Lehner published two books and, according to MathSciNet, a total of 67 research papers with five arising from his work in defense. Furthermore, he published 16 problems and/or solutions in the American Mathematical Monthly. Including Atkin, Lehner had 11 coauthors, with Marvin Knopp and Morris Newman being his most frequent collaborators.

Before meeting Joseph’s father, Lehner’s mother Rachel had been married to Samuel Rapport (abbreviated from the original Rappaport), giving birth to five children before her husband died. She then married Joe’s father, who had had five children by his previous marriage. The family then moved to Massachusetts. Their first child was born at home and soon died. With her second pregnancy, her sister forced her to return to New York City to have her baby at a hospital; this baby was Joe Lehner. For her third and last pregnancy, Joe’s mother again chose to have the birth at home, and the baby died. When Joe was three years old, his parents divorced, and he and his family moved back to New York. As a teenager in New York City, he built a radio, participated on the debate team in high school, and helped one of his half-brothers in his law office, sometimes appearing in court in place of his half-brother. Lehner graduated from high school in 1928 at the age of 15. After a short stay at an experimental college in Wisconsin, he returned home to take courses in mathematics and science at New York University (NYU). While doing so, he obtained a position keeping records at Macy’s which was to last about seven years. Due to the Depression, he lost his job at Macy’s but eventually landed a position on a WPA project, writing his first published paper, “Production, Employment, and Productivity in 57 Selected Industries.” This project took him to Philadelphia in 1936, where he took courses at the University of Pennsylvania that could be transferred to NYU, from which he earned a BS in 1938. Lehner met his future wife, Mary Beluch, in the University of Pennsylvania Library, where she worked as a WPA proofreader. They married on August 17, 1938 and had 65 years together. Mary’s editorial work continued in helping Joe prepare his two books. They had one daughter, Zheindl, nee Janet.

References

The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org, mostly during March and April 2015.

http://arxiv.org/abs/1501.00138
Generalization of Lambert W–function, Bessel polynomials and transcendental equations
Giorgio Mugnaini

http://arxiv.org/abs/1503.02147
Padé interpolation and hypergeometric series
Masatoshi Noumi

http://arxiv.org/abs/1503.02226
Fourier–Bessel heat kernel estimates
Jacek Malecki, Grzegorz Serafin, Tomasz Zorawik

Some inequalities for the trigamma function in terms of the digamma function
Feng Qi, Cristinel Mortici

The asymptotics of a generalised Beta function
R. B. Paris

Darboux transformations for multivariate orthogonal polynomials
Gerardo Ariznabarreta, Manuel Mañas

http://arxiv.org/abs/1503.04972
Some new inequalities for the gamma function
Xiaodong Cao

http://arxiv.org/abs/1503.05003
Darboux transformations for CMV matrices
M.J. Cantero, F. Marcellán, L. Moral, L. Velázquez

Asymptotic properties of biorthogonal polynomials systems related to Hermite and Laguerre polynomials
Yan Xu

Generalizations of Some Inequalities for the $p$–Gamma, $q$–Gamma and $k$–Gamma Functions
Kwara Nantomah, Edward Prempeh
The monic Laguerre polynomials preserve real-rootedness
Praveen S. Venkataramana

Orthogonal polynomials on the disk in the absence of finite moments
Peter C. Gibson

Nicholson–type integrals for products of parabolic cylinder functions involving Laplace
transform of confluent hypergeometric functions
Ridha Nasri

The asymptotic expansion of a generalisation of the Euler–Jacobi series
R.B. Paris

On (p,q)–analogue of Bernstein Operators
M. Mursaleen, Khursheed J. Ansari, Asif Khan

Characterization of the Generalized Chebyshev Polynomials of First Kind
Mohammad A. AlQudah

Selberg integrals, Askey–Wilson polynomials and lozenge tilings of a hexagon with a tri-
angular hole
Hjalmar Rosengren

Special polynomials related to the supersymmetric eight–vertex model: A summary
Hjalmar Rosengren

Generalized Chebyshev I–Bernstein bases transformation
Mohammad A. AlQudah

Asymptotic expansions of zeros of a partial theta function
Vladimir Petrov Kostov

On the spectrum of a partial theta function
Vladimir Petrov Kostov

Generalized Tschebyscheff polynomials of the second kind
Mohammad A. AlQudah
http://arxiv.org/abs/1504.01238
On convergence of basic hypergeometric series
Toshio Oshima

http://arxiv.org/abs/1504.01524
A property of a partial theta function
Vladimir Petrov Kostov

http://arxiv.org/abs/1504.01658
Tschebyscheff of the second kind and Bernstein polynomials change of bases
Mohammad A. AlQudah

http://arxiv.org/abs/1504.01769
Zeros of random functions generated with de Branges kernels
Jorge Antezana, Jordi Marzo, Jan-Fredrik Olsen

http://arxiv.org/abs/1504.01946
Orthogonal Polynomials appearing in SIE grid representations
Stefan Hilger

On Some Hypergeometric Summations II. Duality and Reciprocity
Katsunori Iwasaki

http://arxiv.org/abs/1504.03297
Differential orthogonality: Laguerre and Hermite cases with applications
J. Borrego-Morell, H. Pijeira-Cabrera

http://arxiv.org/abs/1504.03825
On an Orbifold Hamiltonian Structure for the First Painlevé Equation
Katsunori Iwasaki, Shu Okada

http://arxiv.org/abs/1504.03968
Christoffel functions with power type weights
Tivadar Danka, Vilmos Totik

http://arxiv.org/abs/1504.05786
On the double zeros of a partial theta function
Vladimir Petrov Kostov

http://arxiv.org/abs/1504.05976
Asymptotics of orthogonal polynomials generated by a Geronimus perturbation of the Laguerre measure
Alfredo Deaño, Edmundo J. Huertas, Pablo Román

http://arxiv.org/abs/1504.06072
A Lagrangian Method for Deriving New Indefinite Integrals of Special Functions
John T. Conway
Christoffel functions on Jordan curves with respect to measures with jump singularity
Tivadar Danka

Turán type inequalities for regular Coulomb wave functions
Árpád Baricz

The kissing polynomials and their Hankel determinants
Alfredo Deaño, Daan Huybrechs, Arieh Iserles

Fractional integral and generalized Stieltjes transforms for hypergeometric functions as transmutation operators
Tom H. Koornwinder

A Method of Proving a Class of Trigonometric Inequalities Based on Approximations of the Sine and Cosine Functions by Maclaurin Polynomials
Branko Malesevic, Milica Makragic

Hankel Determinant Approach to Generalized Vorob’ev–Yablonski Polynomials and their Roots
Ferenc Balogh, Marco Bertola, Thomas Bothner

Properties of the zeros of generalized basic hypergeometric polynomials
Oksana Bihun, Francesco Calogero

A Riemann–Hilbert problem for equations of Painlevé type in the one matrix model with semi–classical potential
Max R. Atkin

On a family of polynomials related to \((2,1) = (3)\)
Wadim Zudilin

Hypergeometric/Difference–Equation–Based Separability Probability Formulas and Their Asymptotics for Generalized Two–Qubit States Endowed with Random Induced Measure
Paul B. Slater

Weighted Hurwitz numbers and hypergeometric \(-\)functions: an overview
J. Harnad
CM periods, CM regulators and hypergeometric functions, I
Masanori Asakura, Noriyuki Otsubo

CM periods, CM regulators and hypergeometric functions, II
Masanori Asakura, Noriyuki Otsubo

Hypergeometric series, modular linear differential equations, and vector–valued modular forms
Cameron Franc, Geoffrey Mason

http://arxiv.org/abs/1504.03438
A complete Riemann zeta distribution and the Riemann hypothesis
Takashi Nakamura

http://arxiv.org/abs/1504.08058
On Littlewood Polynomials
Raphael Renya, Steven Damelin

http://arxiv.org/abs/1504.07944
Jacobi polynomials and congruences involving some higher–order Catalan numbers and binomial coefficients
Khodabakhsh Hessami Pilehrood, Tatiana Hessami Pilehrood

http://arxiv.org/abs/1504.05801
Some identities of symmetry for q–Euler polynomials under the symmetric group of degree n arising from fermionic p–adic q–integrals on Zp
Dmitry V. Dolgy, Dae San Kim, Taekyun Kim

http://arxiv.org/abs/1504.05499
Some identities of symmetry for q–Bernoulli polynomials under symmetric group of degree n
Dae san Kim, Taekyun Kim

http://arxiv.org/abs/1504.05355
CLT for the zeros of Kostlan Shub Smale random polynomials
Federico Dalmao

http://arxiv.org/abs/1504.03856
Sparse multivariate polynomial interpolation in the basis of Schubert polynomials
Priyanka Mukhopadhyay, Youming Qiao

http://arxiv.org/abs/1504.03705
Racah Polynomials and Recoupling Schemes of \( su(1,1) \)
S. Post

http://arxiv.org/abs/1504.03311
Quantum Hurwitz numbers and Macdonald polynomials
J. Harnad
From: OP–SF NET Editors  
Subject: About the Activity Group

The SIAM Activity Group on Orthogonal Polynomials and Special Functions consists of a broad set of mathematicians, both pure and applied. The Group also includes engineers and scientists, students as well as experts. We have around 115 members scattered about in more than 20 countries. Whatever your specialty might be, we welcome your participation in this classical, and yet modern, topic. Our WWW home page is: http://math.nist.gov/opsf

This is a convenient point of entry to all the services provided by the Group. Our Webmaster is Bonita Saunders (bonita.saunders@nist.gov).

The Activity Group sponsors OP–SF NET, an electronic newsletter, and SIAM-OPSF (OP–SF Talk), a listserv, as a free public service; membership in SIAM is not required. OP–SF NET is transmitted periodically through a post to OP–SF Talk. The OP–SF NET Editors are Howard Cohl (howard.cohl@nist.gov) and Kerstin Jordaan (kerstin.jordaan@up.ac.za).

Back issues of OP–SF NET can be obtained at the websites: https://staff.fnwi.uva.nl/t.h.koornwinder/opsfnet  
http://math.nist.gov/~DLozier/OPSFnet
SIAM-OPSF (OP–SF Talk), which was recently moved to a SIAM server, facilitates communication among members and friends of the Activity Group. To subscribe or to see a link to the archive of all messages, go to http://lists.siam.org/mailman/listinfo/siam-OPSF and follow the instructions under the sub-heading “Subscribing to SIAM-OPSF”. To contribute an item to the discussion, send e-mail to siam-opsf@siam.org. The moderators are Bonita Saunders (bonita.saunders@nist.gov) and Diego Dominici (dominicd@newpaltz.edu).

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phone: +1–215–382–9800  
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Topic #9  OP–SF Net 22.3   May 15, 2015

From: OP–SF NET Editors  
Subject: Submitting contributions to OP–SF NET and SIAM–OPSF (OP–SF Talk)

To contribute a news item to OP–SF NET, send e-mail to one of the OP–SF Editors howard.cohl@nist.gov or kerstin.jordaan@up.ac.za.

Contributions to OP–SF NET 22.4 should be sent by July 1, 2015.

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WWW home page of this Activity Group:  
http://math.nist.gov/opsf  
Information on joining SIAM and this activity group: service@siam.org

The elected Officers of the Activity Group (2014–2016) are:
  Walter Van Assche, Chair
  Jeff Geronimo, Vice Chair
  Diego Dominici, Program Director
  Yuan Xu, Secretary
The appointed officers are:
  Howard Cohl, OP–SF NET co-editor
  Kerstin Jordaan, OP–SF NET co-editor
  Diego Dominici, OP–SF Talk moderator
  Bonita Saunders, Webmaster and OP–SF Talk moderator

Thought of the month

“A ten minute nap in a colloquium is equivalent to one hour of a good night’s sleep.”
by Richard Askey