# O P-S F N E T - Volume 24, Number 1 - January 15, 2017

The Electronic News Net of the SIAM Activity Group on Orthogonal Polynomials and Special Functions

# http://math.nist.gov/opsf

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- 2. Report by a Texas A&M PhD student on the ICMAA meeting in Roorkee, India
- 3. A special function concordance initiative from the IMKT
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# Calendar of Events:

# January 30-February 3, 2017

Biennial Congress of the Royal Spanish Mathematical Society University of Zaragoza, Zaragoza, Spain

http://oventes.rsme.os/ge/zez2017.htm

http://eventos.rsme.es/go/zgz2017.html

Special session on Special functions, orthogonal polynomials and applications, organized by Manuel Alfaro and Antonio Durán,

http://eventos.rsme.es/4762/section/4405/congreso-bienal-de-la-real-sociedad-matematica-espanola.html

# March 20-24, 2017

Elliptic Hypergeometric Functions in Combinatorics, Integrable Systems and Physics Erwin Schrödinger Institute, Vienna, Austria http://www.esi.ac.at/activities/events/2017/elliptic-hypergeometric-functions

# April 19-22, 2017

Optimal Point Configurations and Orthogonal Polynomials Centro Internacional de Encuentros Matemáticos (CIEM), Castro Urdiales, Cantabria, Spain http://www.opcop2017.unican.es

### May 9-12, 2017

The VI Iberoamerican Workshop on Orthogonal Polynomials and Applications (EIBPOA 2017) Universidade Federal do Triângulo Mineiro, Uberaba, MG, Brazil http://eibpoa2017.weebly.com

## June 5-9, 2017

International Conference on Special Functions: Theory, Computation, and Applications City University of Hong Kong, Hong Kong http://www6.cityu.edu.hk/rcms/icsf2017/index.htm

### June 26-30, 2017

OPSF-S7 Summer School on Orthogonal Polynomials and Special Functions, University of Kent, Canterbury, UK https://blogs.kent.ac.uk/opsf-summerschool

### July 3-7, 2017

14<sup>th</sup> International Symposium on Orthogonal Polynomials, Special Functions and Applications (OPSFA14), University of Kent, Canterbury, UK http://www.kent.ac.uk/smsas/personal/opsfa

# July 9-15, 2017

The XVII<sup>th</sup> International Conference on Symmetry Methods in Physics, Yerevan State University, Yerevan, Armenia http://theor.jinr.ru/~symphys/2017

# July 10-15, 2017

Computational Methods and Function Theory, Maria Curie–Skłodowska University, Lublin, Poland http://cmft2017.umcs.lublin.pl

# July 10-19, 2017

Foundations of Computational Mathematics, Barcelona, Spain http://www.ub.edu/focm2017/index.html

Topic #1 \_\_\_\_\_ OP – SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: Walter Van Assche (Walter.VanAssche@wis.kuleuven.be) Subject: SIAG-OPSF election results

Jim Crowley, executive director of SIAM, has informed me of the results of the election for the offices of the SIAM Activity Group "Orthogonal Polynomials and Special Functions".

Elected Name	Position	E-mail Address
Walter Van Assche	Chair	walter@wis.kuleuven.be
Andrei Martínez-Finkelshtein	Vice-Chair	andrei@ual.es
Sarah Post	Program Director	spost@hawaii.edu
Yuan Xu	Secretary	yuan@uoregon.edu

I thank the members of our activity group for the confidence they have in me and Yuan for continuing our offices, and I welcome Andrei and Sarah as new officers. I look forward to working with them the next three years. The term of the elected officers starts January 1, 2017 and runs until December 31, 2019.

The past three years I had the pleasure to have Jeff Geronimo as vice-chair and Diego Dominici as program director. Many thanks for the service you gave to SIAG-OPSF and of course feel free to contact the new officers if you like to share some of your experiences and ideas.

My thanks also goes to all the nominated candidates. Your willingness for making some of your time available to serve the activity group is highly appreciated. We hope that you will still be available to our activity group in the future.

Topic #2 \_\_\_\_\_ OP – SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: Mahishanka Withanachchi (mahiwith@math.tamu.edu) Subject: Report by a Texas A&M PhD student on the ICMAA meeting in Roorkee, India

First of all, I would like to thank SIAM for providing a travel grant to attend the International Conference on Mathematical Analysis and Applications (ICMAA 2016) and I also would like to thank Linda Thiel, SIAM director of programs and services and Walter Van Assche for facilitating my grant as quickly as possible.

Since I have not been able to attend any conferences in India, I was curious about the ICMAA conference and what the Indian Institute of Technology of Roorkee (IIT Roorkee) had to offer me during this 5 day conference. It didn't take long to realize that I was the only graduate student attending the conference from the United States and it was my pleasure to talk with so many great mathematicians from all over the world and share my views with them. Now, without



any hesitation, I can tell that this is one of the best conferences I attended so far in my career as a third year graduate student at Texas A&M University.

I really enjoyed the keynote talk of Walter Van Assche about multiple orthogonal polynomials. It was fascinating how one could use this approach to show the irrationality of the zeta function at specific integer values. I also enjoyed the plenary talks about Bohr's inequality and about univalent analytic, harmonic mappings in the complex plane. I could easily write a few pages about the talks I attended and how they may impact my research in the future, but I would like to save space and say I enjoyed all the talks that came close to my research interests.

My heartfelt gratitude goes to Anbhu Swaminathan and the organizing committee for

having this wonderful conference. I was very pleased to experience great Indian food and accommodation for five days, not to forget the extra effort Dr. Swaminathan had gone through to arrange the transportation back and forth from New Delhi to Roorkee, which took about 6 hours of driving in chaotic traffic. I'm sure all the invited participants enjoyed their time in Roorkee, based on discussions I had during the conference.

Finally, I would like to thank SIAM again for supporting graduate students in every possible way. I wish SIAM and specially the activity group of Orthogonal Polynomials and Special Functions to keep continuing this great work and I look forward to return this generosity to our research community via research and teaching in the future.

Topic #3 \_\_\_\_\_ OP - SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: Patrick D. F. Ion (pion@umich.edu)

Subject: A special function concordance initiative from the IMKT

Recently the Alfred P. Sloan Foundation provided initial funding to set up the International Mathematical Knowledge Trust (IMKT), an organization committed to working toward the dream of a Global Digital Mathematics Library (GDML) endorsed by the International Mathematical Union in 2006. The PIs are Ingrid Daubechies (Duke U, North Carolina, USA) and Stephen Watt (U Waterloo, Ontario, Canada); the IMKT office will be in Waterloo. The proposal resulted from the work of the IMU's GDML Working Group.

A first initiative from the IMKT is to start a Special Functions Concordance. The mathematical community, researchers and users, will find such a resource useful in ensuring clarity for a widely used class of mathematical results. In addition, a concordance will be of value in exploring the capture of the semantics of a mathematical subject area in ways that can make use of, and be used by, computers. In this case, we have a subject that is commonly thought well explored and mostly settled, though clearly the readership here knows there's a lot yet to be done.

Goals we would like a Special Functions Concordance to achieve are:

- to provide a reliable public online resource of special functions (SF) definitions based on recognized community consensus
- to ensure that assertions of SF properties, such as identities between expressions involving SF, are checked and tested on a large scale by allowing comparison between evaluations in different symbolic systems and also numerically
- to be an example of mathematical knowledge disseminated with openness, clear provenance and warranties in a computable manner with modern tools, and so to display a step toward a GDML using modern tools and publication methods

A simple reminder is perhaps in order that there are matters for which it is useful to have publicly agreed upon and well specified conventions for computer handling. We need only think of the differences in published papers and computational systems that lead to varying results, sometimes in ways not obvious to their users: different normalizations in definitions, different conventions in cut choices (e.g., for inverse trigonometric functions), different choices for fundamental parameters (e.g., for elliptic functions), etc.

A possible outline of the development stages of a Special Functions Concordance is:

- 1. Carry out an inventory of SF occurrences in the main resources in the world that offer definitions and representation of SF.
- 2. Develop a corpus of reference definitions; this should be kept by a neutral broker of technical information. Associated with the definitions will be properties and relationships widely asserted and accepted, as well as information as to which systems contain them, and what the differences are between systems when they occur.
- 3. Add to the definitions collected corresponding expressions in standard mathematical data formats, with the various common syntaxes represented.
- 4. Carry out bulk verifications of properties and identities claimed for the SF in the knowledge base developed.
- 5. Record, as they become available, representations of the SF in various formal frameworks and check the property assertions within the formal systems.

The work that has to be done over these stages is not all equally demanding. An early rough inventory probably does not require additional funding but only voluntary collaboration. Settling on definitions will require checking of draft lists and conference calls, at least. The same is true of adding computable expressions. Doing a systematic and comprehensive job of both these activities will require some funding in the medium term. Setting up a bulk testing and verification system, then processing material through it, is also a task that needs resources.

So far, there have been some initial contacts with significant stakeholders in the world of Special Functions (e.g., NIST DLMF, Wolfram Research, Maple, INRIA DDMF, NAG, Sage and some academics). There should soon be a mailing-list set up and further teleconferencing to involve more of the community in both planning and doing. A useful concordance can only be achieved with collaboration and understanding by many committed experts.

To express interest in this initiative or to volunteer to help, e-mail sf-concord@imkt.org, or enquiries to Patrick D. F. Ion (pion@umich.edu), Chair of IMU/Committee on Electronic Information and Communication, GDML Working Group.

Topic #4 \_\_\_\_\_ OP - SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: Tom Koornwinder (T.H.Koornwinder@uva.nl) Subject: Published obituary on Mizan Rahman

Tom Koornwinder would like to inform the readership of OP-SF Net that the following obituary by Mourad Ismail and Erik Koelink on Mizan Rahman was published.

"In memoriam: Mizan Rahman" by Mourad E.H. Ismail and Erik Koelink (including publication list), Journal of Approximation Theory, **201** (2016), 87–97; http://dx.doi.org/10.1016/j.jat.2015.09.001

From: Tom Koornwinder (T.H.Koornwinder@uva.nl)

Subject: Jackson's third *q*-Bessel function versus the Hahn-Exton *q*-Bessel function

It is well known [1] that names of functions in our field are often historically incorrect. If these names are already in use for a long time then it is impossible to still change them in the light of later historical findings. But if the historically incorrect name was introduced more recently then there is still some chance to change the name and give credit to the person who first introduced the function. Here I want to make a case for Jackson's third *q*-Bessel function rather than Hahn-Exton *q*-Bessel function.

In our (Swarttouw and me) 1992 paper [2] (please refer also to the slightly corrected version [3] on arXiv in 2012) we traced back the third q-Bessel function to Hahn (1953) in a special case and Exton (1978) in general. So we introduced the name Hahn–Exton *q*–Bessel function, and this name was also used in the subsequent literature. But later Mourad Ismail [4, p. 184] found these functions already in a paper by Jackson [5, p. 201] in 1904. This was reason for him to propose the name Jackson's third q-Bessel function, and this name has been used since then in quite some papers. But the name with Hahn-Exton also persists in papers until the present day. Please use the name with Jackson in future. Of course you may also mention the earlier name when you introduce the function in the paper.

# References

[1] R. Askey, Discussion of Szegő's paper "An outline of the history of orthogonal polynomials, in: G. Szegő, Collected works, Vol. 3, Birkhäuser, 1982, pp. 866-869.

[2] T. H. Koornwinder and R. F. Swarttouw, On *q*-Analogues of the Fourier and Hankel transforms, Trans. Amer. Math. Soc. 333 (1992), 445-461. doi:10.2307/2154118.

[3] corrected version of [2], arXiv:1208.2521.

[4] M. E. H. Ismail, D. R. Masson and S. K. Suslov, The *q*-Bessel function on a *q*-quadratic grid, in: Algebraic methods and *q*-special functions, CRM Proc. Lecture Notes 22, Amer. Math. Soc., 1999, pp. 183-200. MR 1726835.

[5] F. H. Jackson, The application of basic numbers to Bessel's and Legendre's functions, Proc. London Math. Soc. (2) 2 (1904), 192-220. doi:10.1112/plms/s2-2.1.192.

Topic #6 \_\_\_\_\_ OP - SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: OP-SF Net Editors Subject: Preprints in arXiv.org

The following preprints related to the fields of orthogonal polynomials and special functions were posted or cross-listed to one of the subcategories of arXiv.org during November and December 2016. This list has been separated into two categories.

# **OP-SF Net Subscriber E-Prints**

#### http://arxiv.org/abs/1611.00548

A uniform asymptotic expansion for the incomplete gamma functions revisited R. B. Paris

### http://arxiv.org/abs/1611.01020

Relative Szegő asymptotics for Toeplitz determinants Maurice Duits, Rostyslav Kozhan

### http://arxiv.org/abs/1611.02217

Wronskians of theta functions and series for  $1/\pi$  Alex Berkovich, Heng Huat Chan, Michael J. Schlosser

### http://arxiv.org/abs/1611.02560

Bôcher and abstract contractions of 2nd order quadratic algebras M. A. Escobar Ruiz, E. G. Kalnins, W. Miller, Jr., E. Subag

### http://arxiv.org/abs/1611.03547

CMV biorthogonal Laurent polynomials. II: Christoffel formulas for Geronimus-Uvarov perturbations Gerardo Ariznabarreta, Manuel Mañas, Alfredo Toledano

### http://arxiv.org/abs/1611.03831

Supersymmetric Casimir Energy and  $SL(3, \mathbb{Z})$  Transformations Frederic Brünner, Diego Regalado, Vyacheslav P. Spiridonov

### http://arxiv.org/abs/1611.04973

Macdonald symmetry at q = 1 and a new class of inv-preserving bijections on words Maria Gillespie, Ryan Kaliszewski, Jennifer Morse

### http://arxiv.org/abs/1611.05256

Some elementary observations on Narayana polynomials and related topics II: *q*-Narayana polynomials Johann Cigler

#### http://arxiv.org/abs/1611.05285

Connection formulas for the Ablowitz-Segur solutions of the inhomogeneous Painlevé II equation

Dan Dai, Weiying Hu

### http://arxiv.org/abs/1611.05696

Laplace-type integral representations of the generalized Bessel function and of the Dunkl kernel of type  $B_2$ Bechir Amri, Nizar Demni

### http://arxiv.org/abs/1611.05775

Explicit (Polynomial!) Expressions for the Expectation, Variance and Higher Moments of the Size of a (2n + 1, 2n + 3)-core partition with Distinct Parts Anthony Zaleski, Doron Zeilberger

Log-concavity and Turán-type inequalities for the generalized hypergeometric function S. I. Kalmykov, D. B. Karp

### http://arxiv.org/abs/1611.08028

A fast and spectrally convergent algorithm for fractional integral and differential equations with half-integer order terms Nick Hale, Sheehan Olver

### http://arxiv.org/abs/1611.08064

Two families of orthogonal polynomials on the unit circle from basic hypergeometric functions A. Sri Ranga

#### http://arxiv.org/abs/1611.08806

Hypergeometric heritage of W.N. Bailey. With an appendix: Bailey's letters to F. Dyson Wadim Zudilin

### http://arxiv.org/abs/1611.08932

Spherical functions approach to sums of random Hermitian matrices Arno B. J. Kuijlaars, Pablo Román

### http://arxiv.org/abs/1611.09250

The q-Onsager algebra and multivariable q-special functions Pascal Baseilhac, Luc Vinet, Alexei Zhedanov

#### http://arxiv.org/abs/1611.09486

Between the stochastic six vertex model and Hall-Littlewood processes Alexei Borodin, Alexey Bufetov, Michael Wheeler

### http://arxiv.org/abs/1612.00051

Images of Maass-Poincaré series in the lower half-plane Nickolas Andersen, Kathrin Bringmann, Larry Rolen

### http://arxiv.org/abs/1612.01149

Nikishin systems on star-like sets: ratio asymptotics of the associated multiple orthogonal polynomials Abey López-García, Guillermo López Lagomasino

#### http://arxiv.org/abs/1612.01486

A linear system of differential equations related to vector-valued Jack polynomials on the torus Charles F. Dunkl

### http://arxiv.org/abs/1612.01916

Large gap asymptotics at the hard edge for product random matrices and Muttalib-Borodin ensembles Tom Claeys, Manuela Girotti, Dries Stivigny

Extended relativistic Toda lattice and L-orthogonal polynomials on the real line and on the unit circle Cleonice F. Bracciali, Jairo S. Silva, A. Sri Ranga

### http://arxiv.org/abs/1612.02257

On the Laplace transform of absolutely monotonic functions Stamatis Koumandos, Henrik L. Pedersen

### http://arxiv.org/abs/1612.03718

Orthogonal expansions related to compact Gelfand pairs Christian Berg, Ana P. Peron, Emilio Porcu

#### http://arxiv.org/abs/1612.04038

Tridiagonal representations of the q-oscillator algebra and Askey-Wilson polynomials Satoshi Tsujimoto, Luc Vinet, Alexei Zhedanov

#### http://arxiv.org/abs/1612.05051

Rahman's biorthogonal functions and superconformal indices Hjalmar Rosengren

#### http://arxiv.org/abs/1612.05301

A transference result of the  $L^p$  continuity of the Jacobi Littlewood–Paley g-function to the Gaussian and Laguerre Littlewood–Paley g-function Eduard Navas, Wilfredo Urbina

#### http://arxiv.org/abs/1612.05455

On the Weber integral equation and solution to the Weber-Titchmarsh problem Semyon Yakubovich

#### http://arxiv.org/abs/1612.05514

Durfee rectangles and pseudo-Wronskian equivalences for Hermite polynomials David Gómez-Ullate, Yves Grandati, Robert Milson

#### http://arxiv.org/abs/1612.07035

Applications of spectral theory to special functions Erik Koelink

http://arxiv.org/abs/1612.07108

Riemann-Hilbert analysis for a Nikishin system Guillermo López Lagomasino, Walter Van Assche

#### http://arxiv.org/abs/1612.07229

Generalized Sobolev orthogonal polynomials, matrix moment problems and integrable systems Gerardo Ariznabarreta, Manuel Mañas, Piergiulio Tempesta

#### http://arxiv.org/abs/1612.07284

q-Analogues of two product formulas of hypergeometric functions by Bailey Michael J. Schlosser

Invariant properties for Wronskian type determinants of classical and classical discrete orthogonal polynomials under an involution of sets of positive integers Guillermo P. Curbera, Antonio J. Durán

### http://arxiv.org/abs/1612.07686

The Wigner distribution function for the  $\mathfrak{su}(2)$  finite oscillator and Dyck paths Roy Oste, Joris Van der Jeugt

### http://arxiv.org/abs/1612.07692

A finite oscillator model with equidistant position spectrum based on an extension of  $\mathfrak{su}(2)$  Roy Oste, Joris Van der Jeugt

### http://arxiv.org/abs/1612.07700

A finite quantum oscillator model related to special sets of Racah polynomials Roy Oste, Joris Van der Jeugt

### http://arxiv.org/abs/1612.07815

A superintegrable model with reflections on  $S^{n-1}$  and the higher rank Bannai-Ito algebra Hendrik De Bie, Vincent X. Genest, Jean-Michel Lemay, Luc Vinet

### http://arxiv.org/abs/1612.08219

On a modularity conjecture of Andrews, Dixit, Schultz, and Yee for a variation of Ramamunjan's  $\omega(q)$ Kathrin Bringmann, Chris Jennings-Shaffer, Karl Mahlburg

### http://arxiv.org/abs/1612.08575

Maximum of the Riemann zeta function on a short interval of the critical line Louis-Pierre Arguin, David Belius, Paul Bourgade, Maksym Radziwiłł, Kannan Soundararajan

### http://arxiv.org/abs/1612.08732

On Asymptotic Regimes of Orthogonal Polynomials with Complex Varying Quartic Exponential Weight Marco Bertola, Alexander Tovbis

#### http://arxiv.org/abs/1612.09196

3nj-symbols and identities for q-Bessel functions Wolter Groenevelt

# **Other Relevant OP-SF E-Prints**

#### http://arxiv.org/abs/1611.00242

On Spectral Approximations With Nonstandard Weight Functions and Their Implementations to Generalized Chaos Expansions Adi Ditkowski, Rami Kats

#### http://arxiv.org/abs/1611.00267

The growth of polynomials orthogonal on the unit circle with respect to a weight w that satisfies  $w, w^{-1} \in L^{\infty}(\mathbb{T})$ Sergey Denisov

Regularity results for transmission problems with sign-changing coefficients: a modal approach Valentin Vinoles

### http://arxiv.org/abs/1611.00438

Properties of the Turánian of modified Bessel functions István Mező, Árpád Baricz

### http://arxiv.org/abs/1611.00734

On the constants for some fractional Gagliardo-Nirenberg and Sobolev inequalities Carlo Morosi, Livio Pizzocchero

### http://arxiv.org/abs/1611.00957

Zeta Series Generating Function Transformations Related to Generalized Stirling Numbers and Partial Sums of the Hurwitz Zeta Function Maxie D. Schmidt

### http://arxiv.org/abs/1611.01274

Evaluation of Log-tangent Integrals by series involving  $\zeta(2n+1)$  Lahoucine Elaissaoui, Zine El Abidine Guennoun

### http://arxiv.org/abs/1611.01356

Circular pentagons and real solutions of Painlevé VI equations Alexandre Eremenko, Andrei Gabrielov

#### http://arxiv.org/abs/1611.01624

On boundary-value problems for a partial differential equation with Caputo and Bessel operators Praveen Agarwal, Erkinjon Karimov, Murat Mamchuev, Michael Ruzhansky

#### http://arxiv.org/abs/1611.02377

Bernoulli, poly-Bernoulli, and Cauchy polynomials in terms of Stirling and r-Stirling numbers Khristo N. Boyadzhiev

#### http://arxiv.org/abs/1611.02467

Confining non-analytic exponential potential  $V(x) = g^2 \exp(2|x|)$  and its exact Bessel-function solvability Ryu Sasaki

#### http://arxiv.org/abs/1611.02668

Computing the Laplace eigenvalue and level of Maass cusp forms Paul Savala

http://arxiv.org/abs/1611.02822 On finite Carlitz multiple polylogarithms Chieh-Yu Chang, Yoshinori Mishiba

#### http://arxiv.org/abs/1611.02889

Hierarchies of sum rules for squares of spherical Bessel functions L. G. Suttorp, A. J. van Wonderen

Asymptotic expansions of the inverse of the Beta distribution Dimitris Askitis

### http://arxiv.org/abs/1611.03697

Riemann-Hilbert problems from Donaldson-Thomas theory Tom Bridgeland

#### http://arxiv.org/abs/1611.04663

Asymptotic formulae of two divergent bilateral basic hypergeometric series Hironori Mori, Takeshi Morita

#### http://arxiv.org/abs/1611.05385

On solutions of ultradiscrete Painlevé II equation with parity variables Hikaru Igarashi, Kouichi Takemura

#### http://arxiv.org/abs/1611.05562

On the extreme values of the Riemann zeta function on random intervals of the critical line Joseph Najnudel

### http://arxiv.org/abs/1611.05952

Symmetric Morse potential is exactly solvable Ryu Sasaki

#### http://arxiv.org/abs/1611.06090

Some Model Theory of Hypergeometric and Pfaffian Functions Ricardo Bianconi

#### http://arxiv.org/abs/1611.06493

Stochastic coagulation-fragmentation processes with a finite number of particles and applications Nathanael Hoze, David Holcman

#### http://arxiv.org/abs/1611.06643

Generalized Lamé equation with finite monodromy You-Cheng Chou

### http://arxiv.org/abs/1611.06872

An elementary proof of the positivity of the intertwining operator in one-dimensional trigonometric Dunkl theory Jean-Philippe Anker

#### http://arxiv.org/abs/1611.06991

Krawtchouk-Griffiths Systems I: Matrix Approach Philip Feinsilver

#### http://arxiv.org/abs/1611.07242

Laplace copulas of multifactor gamma distributions are new generalized Farlie-Gumbel-Morgenstern copulas Philippe Bernardoff

Generalized Rodriguez-Villegas supercongruences involving p-adic Gamma functions Ji-Cai Liu

### http://arxiv.org/abs/1611.08126

On mixed joint discrete universality for a class of zeta-functions Roma Kačinskaitė, Kohji Matsumoto

#### http://arxiv.org/abs/1611.08213

An introduction to Dunkl theory and its analytic aspects Jean-Philippe Anker

#### http://arxiv.org/abs/1611.08423

Inequalities of extended Beta and extended hypergeometric functions Saiful R. Mondal

#### http://arxiv.org/abs/1611.08493

Modular forms, Schwarzian conditions, and symmetries of differential equations in physics Y. Abdelaziz, J.-M. Maillard

#### http://arxiv.org/abs/1611.08693

On The Product of Dedekind zeta functions Soumyarup Banerjee, Azizul Hoque, Kalyan Chakraborty

#### http://arxiv.org/abs/1611.08706

Improved error bound for multivariate Chebyshev polynomial interpolation Kathrin Glau, Mirco Mahlstedt

### http://arxiv.org/abs/1611.08885

The law of large numbers for the maximum of almost Gaussian log-correlated fields coming from random matrices Gaultier Lambert, Elliot Paquette

http://arxiv.org/abs/1611.08971

Conformal blocks and Painlevé functions Hajime Nagoya

http://arxiv.org/abs/1611.09157

Pathway fractional integral operators involving k-Struve function Kottakkaran S. Nisar, Saiful R. Mondal

#### http://arxiv.org/abs/1611.09198

Averages of ratios of the Riemann zeta-function and correlations of divisor sums Brian Conrey, Jonathan P. Keating

http://arxiv.org/abs/1611.09429

More on some Mock theta Double sums Alexander E. Patkowski

On the critical points of random matrix characteristic polynomials and of the Riemann  $\xi$ -function Sasha Sodin

### http://arxiv.org/abs/1611.10188

A p-adic supercongruence for truncated hypergeometric series  $_7F_6$  Ji-Cai Liu

### http://arxiv.org/abs/1611.10192

Controllability of a 2D quantum particle in a time-varying disc with radial data Iván Moyano

#### http://arxiv.org/abs/1611.10325

An effective universality theorem for the Riemann zeta-function Youness Lamzouri, Stephen Lester, Maksym Radziwill

#### http://arxiv.org/abs/1612.00056

Generalized Fourier-Bessel operator and almost-periodic interpolation and approximation Jean-Paul Gauthier, Dario Prandi

### http://arxiv.org/abs/1612.00205

Construction by similarity method of the fundamental solution of the Dirichlet problem for Keldysh type equation in the half-space Oleg D. Algazin

### http://arxiv.org/abs/1612.00588

Krawtchouk-Griffiths Systems II: As Bernoulli Systems Philip Feinsilver

### http://arxiv.org/abs/1612.00726

A note on the universality of Hurwitz-Lerch zeta functions Mattia Righetti

http://arxiv.org/abs/1612.00765

A generalization of Ramanujan's congruence to modular forms of prime level Radu Gaba, Alexandru A. Popa

#### http://arxiv.org/abs/1612.00862

Some Open Problems Concerning Orthogonal Polynomials on Fractals and Related Questions Gökalp Alpan, Alexander Goncharov

http://arxiv.org/abs/1612.00927

Simplified Expressions of the Multi-indexed Laguerre and Jacobi Polynomials Satoru Odake, Ryu Sasaki

#### http://arxiv.org/abs/1612.01141

Multirank and classical theta functions Shishuo Fu, Dazhao Tang

Real solutions of the first Painlevé equation with large initial data Wen-Gao Long, Yu-Tian Li, Sai-Yu Liu, Yu-Qiu Zhao

### http://arxiv.org/abs/1612.01672

On Systolic Zeta Functions Ivan Babenko, Daniel Massart

#### http://arxiv.org/abs/1612.01698

Moments of Hardy's function over short intervals Aleksandar Ivić

### http://arxiv.org/abs/1612.01747

Formulas of Szegő type for the periodic Schrödinger operator Bernhard Pfirsch, Alexander V. Sobolev

#### http://arxiv.org/abs/1612.02117

One-point theta functions for vertex operator algebras Matthew Krauel

### http://arxiv.org/abs/1612.02144

A q-series identity via the  $\mathfrak{sl}_3$  colored Jones polynomials for the (2,2m)-torus link Wataru Yuasa

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Finite Ramanujan expansions and shifted convolution sums of arithmetical functions Giovanni Coppola, M. Ram Murty, Biswajyoti Saha

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K. S. Nisar, J. Choi

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On Jacobian group and complexity of the generalized Petersen graph GP(n, k) through Chebyshev polynomials Y. S. Kwon, A. D. Mednykh, I. A. Mednykh

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Saito duality and the classical theory of arithmetic functions Gennadiy Ilyuta

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Unified Framework for the Effective Rate Analysis of Wireless Communication Systems over MISO Fading Channels Minglei You, Hongjian Sun, Jing Jiang, Jiayi Zhang

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Log-convex and Stieltjes moment sequences Yi Wang, Bao-Xuan Zhu

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Hypergeometric solutions to a three dimensional dissipative oscillator driven by aperiodic forces Alessio Bocci, Giovanni Mingari Scarpello, Daniele Ritelli

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Relating Zeta Functions of Discrete and Quantum Graphs Jonathan Harrison, Tracy Weyand

Commensurability and arithmetic equivalence for orthogonal hypergeometric monodromy groups Jitendra Bajpai, Sandip Singh, Scott Thomson

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An odd variant of multiple zeta values Michael E. Hoffman

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Enumeration of the Chebyshev-Frolov lattice points in axis-parallel boxes Kosuke Suzuki, Takehito Yoshiki

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Integrals of spherical harmonics with Fourier exponents in multidimensions F. Goncharov

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Hypergeometric Euler numbers Takao Komatsu, Huilin Zhu

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On Painlevé/gauge theory correspondence Giulio Bonelli, Oleg Lisovyy, Kazunobu Maruyoshi, Antonio Sciarappa, Alessandro Tanzini

#### http://arxiv.org/abs/1612.06517

Selberg integral theory and Muttalib-Borodin ensembles P. J. Forrester, J. R. Ipsen

#### http://arxiv.org/abs/1612.06563

Weighted sum formulas of multiple zeta values with even arguments Zhonghua Li, Chen Qin

#### http://arxiv.org/abs/1612.06904

Type I integrable defects and finite-gap solutions for KdV and sine-Gordon models E. Corrigan, R. Parini

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Free Energy on a Cycle Graph and Trigonometric Deformation of Heat Kernel Traces on Odd Spheres Nahomi Kan, Kiyoshi Shiraishi

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Traveling wave solutions to Kawahara and related equations Stefan C. Mancas

Analysis of the Fractional Integrodifferentiability of Power Functions and some Identities with Hypergeometric Functions Fabio Grangeiro Rodrigues, Edmundo Capelas de Oliveira

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An extension of the Bernoulli polynomials inspired by the Tsallis statistics M. Balamurugan, R. Chakrabarti, R. Jagannathan

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Confluent Hypergeometric Equation via Fractional Calculus Approach Fabio G. Rodrigues, Edmundo C. Oliveira

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Construction and implementation of asymptotic expansions for Laguerre-type orthogonal polynomials Daan Huybrechs, Peter Opsomer

### http://arxiv.org/abs/1612.08098

On some analytic properties of quaternionic Hermite polynomials K. Diki, A. El Hamyani, A. Ghanmi

### http://arxiv.org/abs/1612.08382

On the connection problem for Painlevé I O. Lisovyy, J. Roussillon

#### http://arxiv.org/abs/1612.08627

Lehmer pairs and derivatives of Hardy's Z-function Aleksander Simonič

### http://arxiv.org/abs/1612.08783

Irrationality of special values of formal Laurent series represented by the formal Mellin transform of G-functions Makoto Kawashima

#### http://arxiv.org/abs/1612.08803

A Neumann series of Bessel functions representation for solutions of Sturm-Liouville equations Vladislav V. Kravchenko, Sergii M. Torba

#### http://arxiv.org/abs/1612.09039

Anatomy of a q-generalization of the Laguerre/Hermite Orthogonal Polynomials Chuan-Tsung Chan, Hsiao-Fan Liu

#### http://arxiv.org/abs/1612.09407

An equivalence between desingularized and renormalized values of multiple zeta functions at negative integers Nao Komiyama

Noncommutative Harmonic Analysis on Quantum Hyperbolic Spaces. The Laplace-Beltrami Operator Olga Bershtein

Topic #7 \_\_\_\_\_ OP - SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: OP-SF Net Editors Subject: About the Activity Group

The SIAM Activity Group on Orthogonal Polynomials and Special Functions consists of a broad set of mathematicians, both pure and applied. The Group also includes engineers and scientists, students as well as experts. We have 176 members (as of October 20, 2016) scattered about in 30 countries. Whatever your specialty might be, we welcome your participation in this classical, and yet modern, topic. Our WWW home page is: http://math.nist.gov/opsf

This is a convenient point of entry to all the services provided by the Group. Our Web-master is Bonita Saunders (bonita.saunders@nist.gov).

The Activity Group sponsors OP-SF NET, an electronic newsletter, and SIAM-OPSF (OP-SF Talk), a listserv, as a free public service; membership in SIAM is not required. OP-SF NET is transmitted periodically through a post to OP-SF Talk. The OP-SF Net Editors are Howard Cohl (howard.cohl@nist.gov), and Sarah Post (spost@hawaii.edu).

Back issues of OP-SF NET can be obtained at the websites: https://staff.fnwi.uva.nl/t.h.koornwinder/opsfnet http://math.nist.gov/~DLozier/OPSFnet

SIAM-OPSF (OP-SF Talk), which was recently moved to a SIAM server, facilitates communication among members and friends of the Activity Group. To subscribe, go to http://lists.siam.org/mailman/listinfo/siam-OPSF and follow the instructions under the sub-heading "Subscribing to SIAM-OPSF". To contribute an item to the discussion, send email to siam-opsf@siam.org. The moderators are Bonita Saunders (bonita.saunders@nist.gov) and Diego Dominici (dominicd@newpaltz.edu).

SIAM has several categories of membership, including low-cost categories for students and residents of developing countries. In addition, there is the possibility of reduced rate membership for the members of several societies with which SIAM has a reciprocity agreement; see http://www.siam.org/membership/individual/reciprocal.php. For current information on SIAM and Activity Group membership, contact:

Society for Industrial and Applied Mathematics 3600 University City Science Center Philadelphia, PA 19104-2688 USA phone: +1-215-382-9800 e-mail: service@siam.org WWW : http://www.siam.org Topic #8 \_\_\_\_\_ OP - SF Net 24.1 \_\_\_\_\_ January 15, 2017

From: OP-SF Net Editors Subject: Submitting contributions to OP-SF NET and SIAM-OPSF (OP-SF Talk)

To contribute a news item to OP-SF NET, send e-mail to one of the OP-SF Editors howard.cohl@nist.gov, or spost@hawaii.edu. Contributions to OP-SF NET 24.2 should be sent by March 1, 2017.

OP-SF NET is an electronic newsletter of the SIAM Activity Group on Special Functions and Orthogonal Polynomials. We disseminate your contributions on anything of interest to the special functions and orthogonal polynomials community. This includes announcements of conferences, forthcoming books, new software, electronic archives, research questions, and job openings as well as news about new appointments, promotions, research visitors, awards and prizes. OP-SF Net is transmitted periodically through a post to SIAM-OPSF (OP-SF Talk).

SIAM-OPSF (OP-SF Talk) is a listserv of the SIAM Activity Group on Special Functions and Orthogonal Polynomials, which facilitates communication among members, and friends of the Activity Group. See the previous Topic. To post an item to the listsery, send e-mail to siam-opsf@siam.org.

WWW home page of this Activity Group: http://math.nist.gov/opsf Information on joining SIAM and this activity group: service@siam.org

The elected Officers of the Activity Group (2014–2016) are: Walter Van Assche, Chair Andrei Martínez-Finkelshtein, Vice Chair Sarah Post, Program Director Yuan Xu, Secretary

The appointed officers are: Howard Cohl, OP-SF NET co-editor Sarah Post, OP-SF NET co-editor Diego Dominici, OP-SF Talk moderator Bonita Saunders, Webmaster and OP-SF Talk moderator

# Thought of the month

"sin<sup>2</sup> $\varphi$  is odious to me, even though Laplace made use of it; should it be feared that sin<sup>2</sup> $\varphi$ might become ambiguous, which would perhaps never occur, or at most very rarely when speaking of  $\sin(\varphi^2)$ , well then, let us write  $(\sin \varphi)^2$ , but not  $\sin^2 \varphi$ , which by analogy should signify  $sin(sin \varphi)$ . "

Carl Friedrich Gauss (1777-1855),

in a letter to astronomer Heinrich Christian Schumacher, September 23, 1839 (much thanks to Juan José Moreno Balcázar, Universidad de Almería, Spain, for pointing out the correct date of the correspondence).